

# PRESUPERNOVA EVOLUTION AND NUCLEOSYNTHESIS OF ROTATING MASSIVE STARS @ VARIOUS METALLICITIES

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PRIN MIUR 2010-2011, project “The Chemical and dynamical Evolution of the Milky Way and Local Group Galaxies”. PI: F. Matteucci

# PRESUPERNOVA EVOLUTIONS

INITIAL MASSES: 13, 15, 20, 25, 30, 40, 60, and 80  $M_{\odot}$

INITIAL COMPOSITIONS:

$[\text{Fe}/\text{H}]=0, Z=1.345 \cdot 10^{-2}$	Asplund et al. 2009
$[\text{Fe}/\text{H}]=-1, Z=3.236 \cdot 10^{-3}$	Scaled solar $\text{Fe}/\text{Fe}_{\odot}=0.1, 0.01, 0.001$
$[\text{Fe}/\text{H}]=-2, Z=3.236 \cdot 10^{-4}$	except
$[\text{Fe}/\text{H}]=-3, Z=3.236 \cdot 10^{-5}$	$[\text{C}/\text{Fe}]=0.18$
	$[\text{O}/\text{Fe}]=0.47$
	$[\text{Mg}/\text{Fe}]=0.27$
	$[\text{Si}/\text{Fe}]=0.37$
	$[\text{S}/\text{Fe}]=0.35$
	$[\text{Ar}/\text{Fe}]=0.35$
	$[\text{Ca}/\text{Fe}]=0.33$
	$[\text{Ti}/\text{Fe}]=0.23$
	(Cayrel+ 2004 and Spite+ 2005)

INITIAL EQUATORIAL VELOCITIES: 0, 150, 300 km/s

# PRESUPERNOVA EVOLUTIONS

All models computed with the **FRANEC (Frascati RAphson Newton Evolutionary Code) 6.0**

Major improvements compared to the release 4.0 (ML & Chieffi 2003) and 5.0 (ML & Chieffi 2006)

- FULL COUPLING of: Physical Structure - Nuclear Burning - Chemical Mixing (convection, semiconvection, rotation)
- INCLUSION OF ROTATION:
  - Shellular Rotation (Meynet & Maeder 1997)
  - Transport of Angular Momentum due to shear instabilities and meridional circulation (Advection/Diffusion equation, Meynet & Maeder 2000)
  - Coupling of Rotation and Mass Loss (angular momentum losses due to stellar wind and mechanical mass losses due to rotation)
- MASS LOSS:
  - OB: Vink et al. 2000,2001
  - RSG: de Jager 1988+Van Loon 2005 (Dust driven wind)
  - WR: Nugis & Lamers 2000
  - Supra Eddington Mass Loss
  - Mechanical mass loss due to rotation (close to critical velocity)

# PRESUPERNOVA EVOLUTIONS

$$\frac{\partial P}{\partial M} = -\frac{GM}{4\pi R^4} f_P$$

$$\frac{\partial R}{\partial M} = \frac{1}{4\pi\rho R^2}$$

$$\frac{\partial T}{\partial M} = -\frac{GMT}{4\pi R^2 P} \nabla \frac{f_T}{f_P}$$

$$\frac{\partial L}{\partial M} = \varepsilon$$

$$\frac{\partial Y_i}{\partial t} = \left( \frac{\partial Y_i}{\partial t} \right)_{\text{nuc}} + \frac{\partial}{\partial m} \left[ (4\pi\rho r^2)^2 (D_{\text{mix}} + D_{\text{semi}} + D_{\text{rot}}) \left( \frac{\partial X_i}{\partial m} \right) \right]$$

FRANEC 6.0: Numerical Scheme

FULL COUPLING and simultaneous solution of: Physical Structure - Nuclear Burning - Chemical Mixing (convection, semiconvection, rotation) equations

$$\rho \frac{d}{dt} (r^2 \omega) = \frac{1}{5r^2} \frac{\partial}{\partial r} (\rho r^4 \omega U) + \frac{1}{r^2} \frac{\partial}{\partial r} \left( \rho D_{\text{shear}} r^4 \frac{\partial \omega}{\partial r} \right)$$

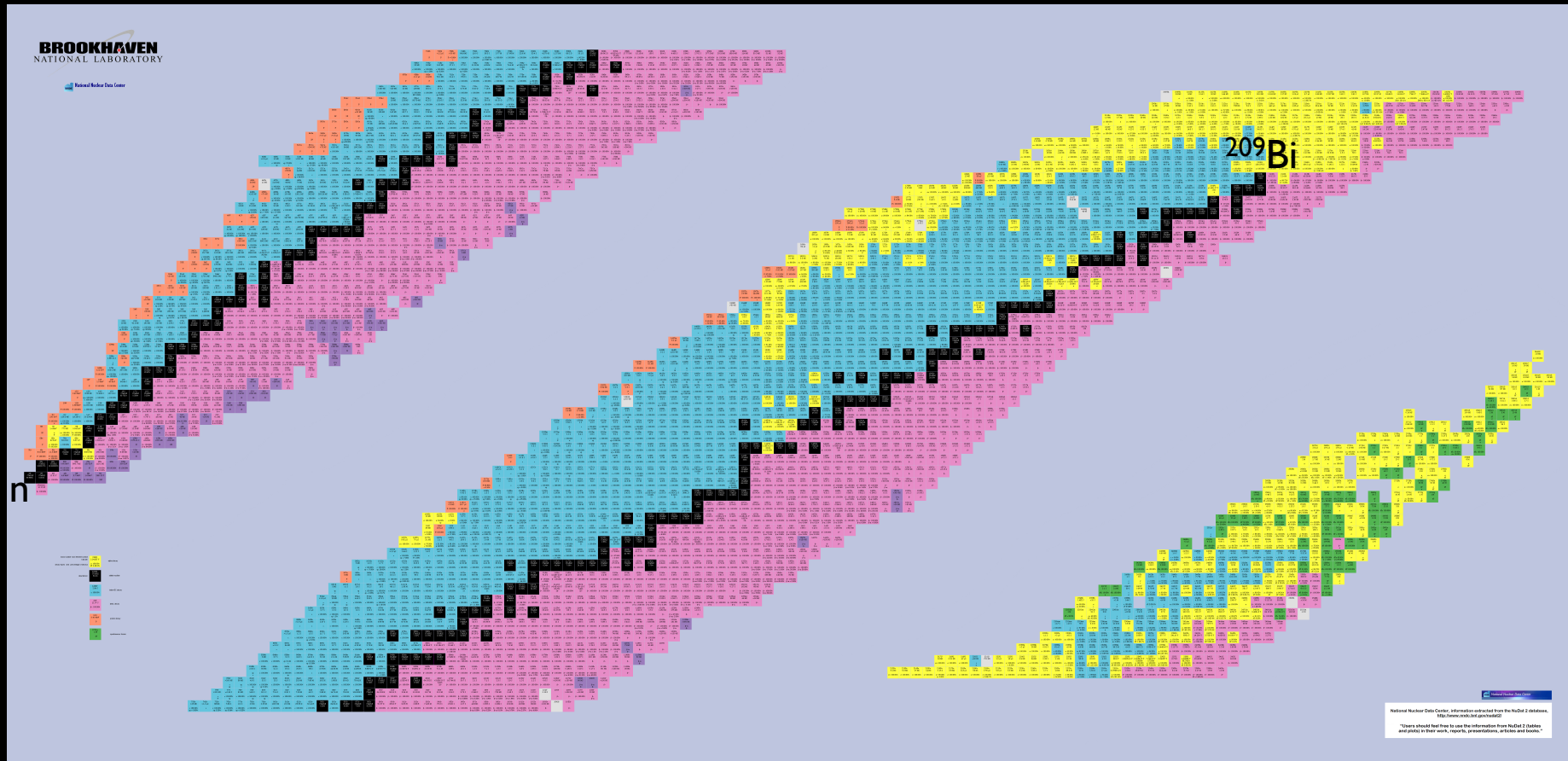
Meridional Circulation

Shear Instabilities

(4<sup>th</sup> order → 4 ODE solved by means of a relaxation method)

# PRESUPERNOVA EVOLUTIONS

## FRANEC 6.0: NUCLEAR NETWORK



- TWO NUCLEAR NETWORKS FULLY COUPLED TO THE EVOLUTION:
  - 200 isotopes from n to  $^{209}\text{Bi}$  (500 reactions) H/He Burning
  - 320 isotopes from n to  $^{209}\text{Bi}$  (3000 reactions) Advanced Burning

# CALIBRATION OF THE ROTATIONAL MIXING EFFICIENCY

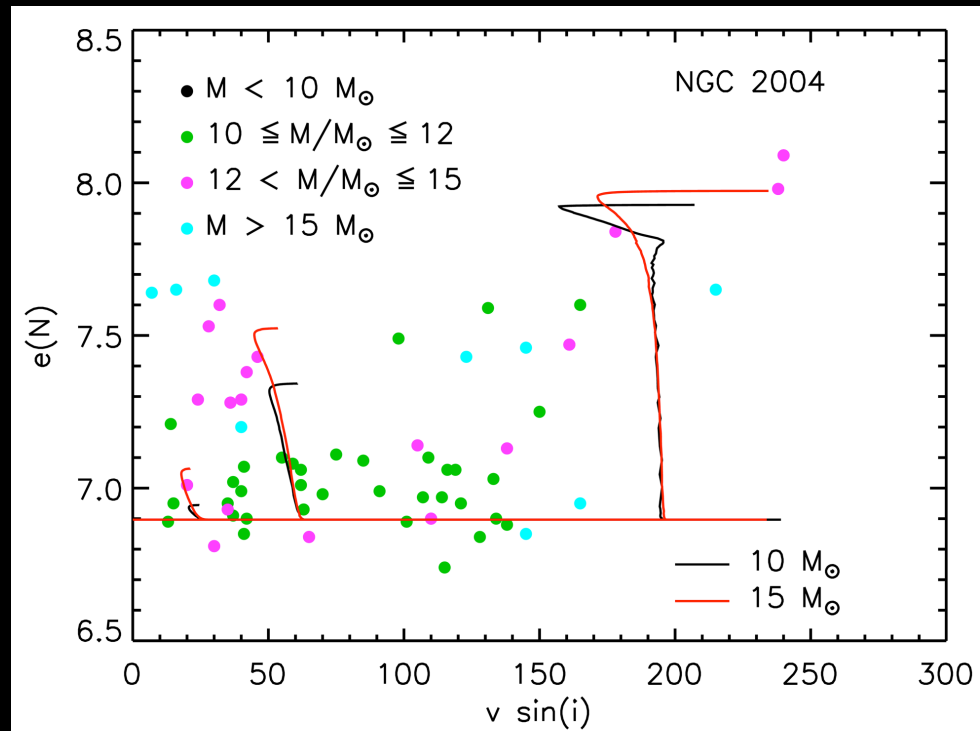
All the uncertainties in the treatment of rotation may be accounted for essentially by means of two free parameters

$f_c$  that multiplies the diffusion coefficient adopted for the mixing of the chemicals

$$D = f_c D_{\text{rot}} = f_c (D_{\text{shear}} + D_{\text{mc}})$$

$f_\mu$  that multiplies the gradient of molecular weight  $\nabla_\mu \rightarrow f_\mu \nabla_\mu$  (Heger+ 2000)

$f_c, f_\mu$  calibrated in order to reproduce the observed nitrogen surface abundances as a function of the projected rotational velocity for stars in the LMC sample (NGC 2004) of the FLAMES survey (Hunter+ 2009)



## DIRECT EFFECTS

### Internal Mixing (meridional circulation, shear diffusion)

- **Larger Cores** and **Longer Evolutionary Times** (these effects are negligible after core He depletion due to the dramatic shortening of the advanced evolutionary phases)
- **Surface enrichment** in elements produced in the innermost zones
- More Compact Structures → **Higher Luminosities**

### Reduction of the Effective Gravity (centrifugal force, angular momentum transport)

- More Expanded Envelopes → **Lower Effective Temperatures**

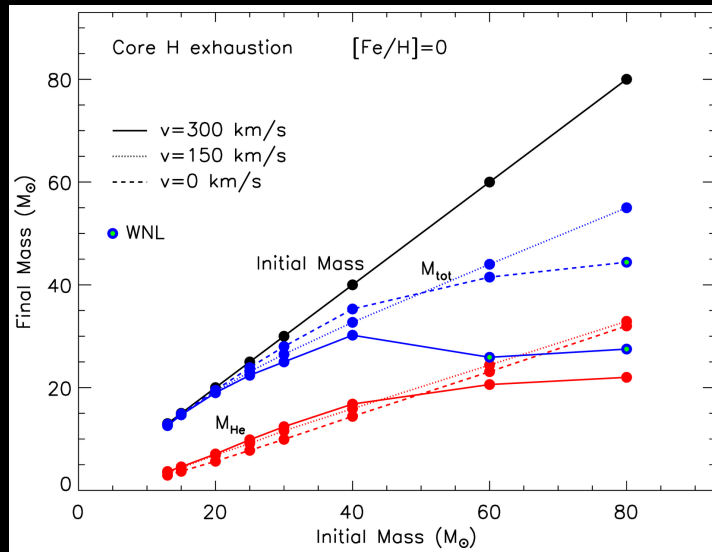
### Mechanical Mass Loss

- **Increase of Mass Loss** if the star reaches the Critical Velocity

## INDIRECT EFFECTS

Higher Luminosities and Lower Effective Temperatures → **Increase of Mass Loss efficiency**

# He Core Mass @ Core H Depletion





## DIRECT EFFECTS

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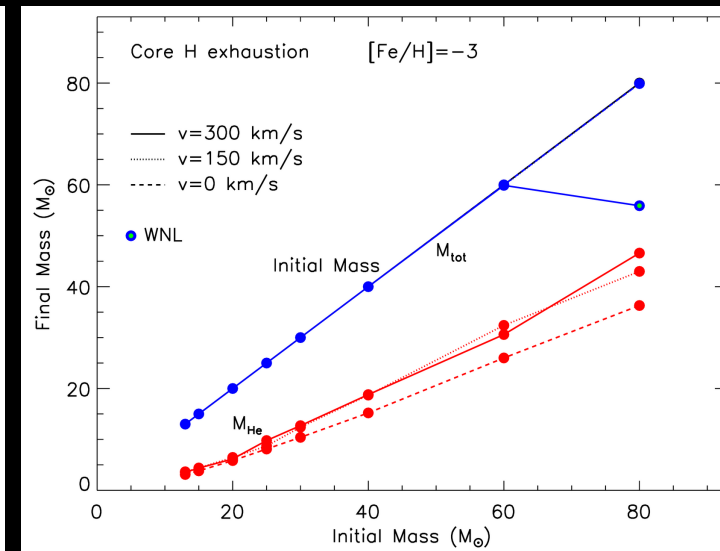
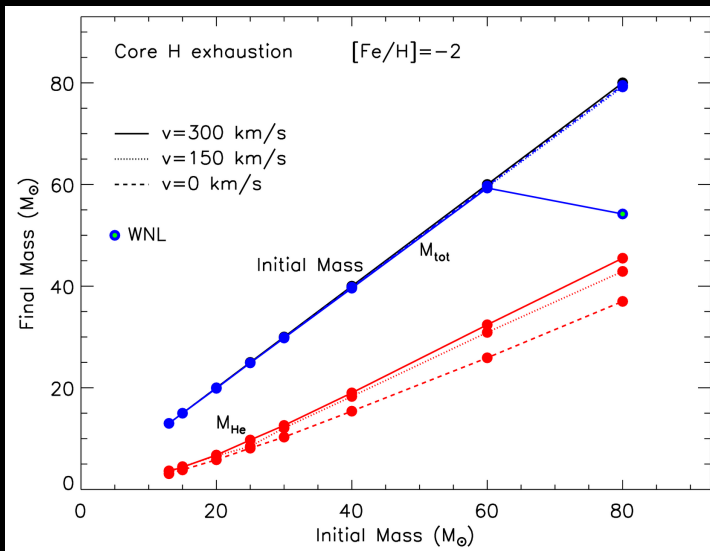
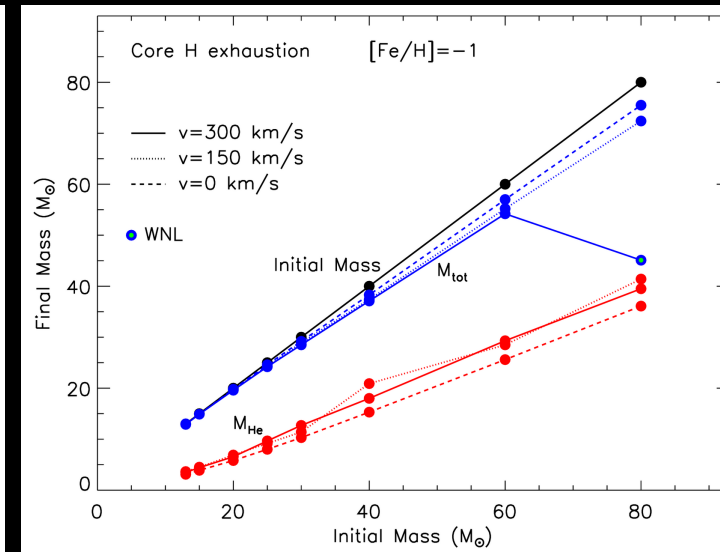
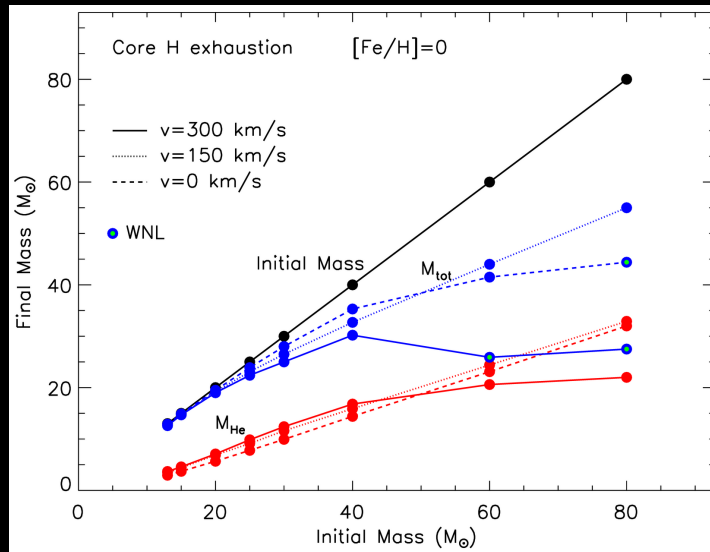
## INDIRECT EFFECTS

Higher Luminosities and Lower Effective Temperatures → **Increase of Mass Loss efficiency**

Decreasing the  
metallicity

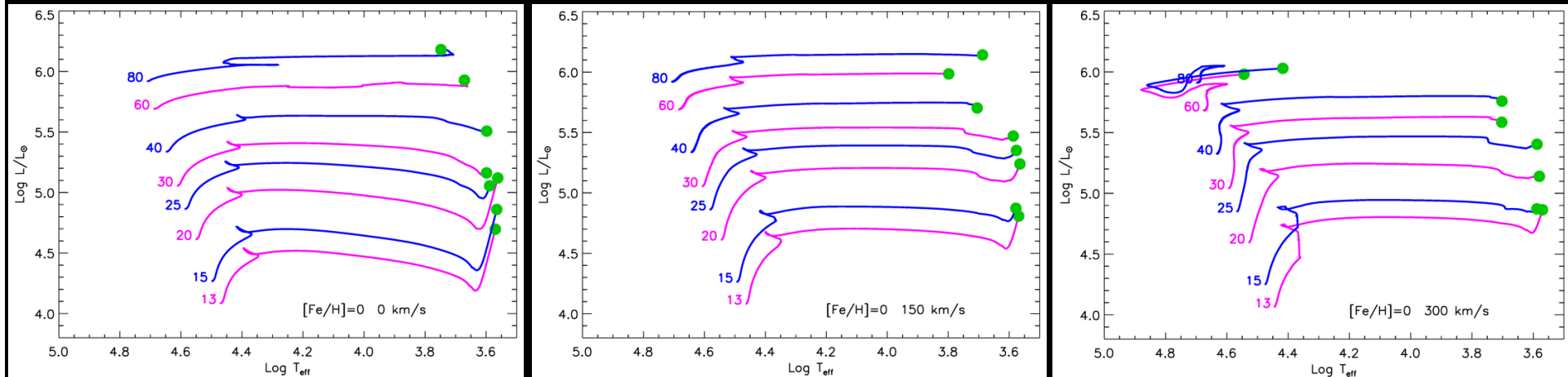


# He Core Mass @ Core H Depletion



## Core He Burning: Solar Metallicity Models

After core H depletion, all the models (except 60 and 80  $M_{\odot}$   $v=300$  km/s) evolve toward a RSG configuration



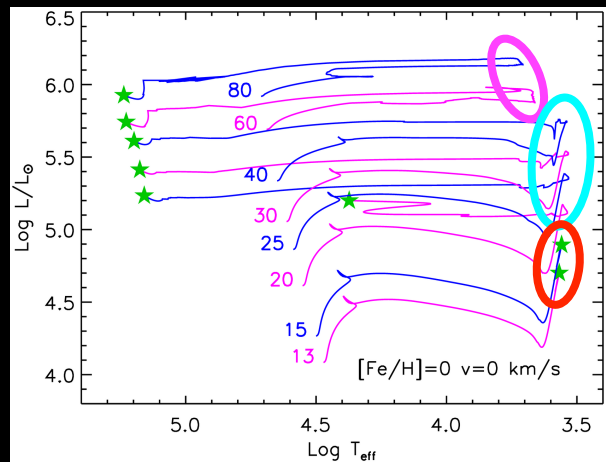
During the following evolution (core He burning)

- The higher mass models may reach the Eddington limit  $\rightarrow$  most of the H-rich envelope is lost and the star evolves to the a BSG configuration
- The lower mass models may become cool enough that dust driven wind becomes very efficient. The central He mass fraction at which this occurs determines how much mass is lost during core He burning and whether the star evolves to a BSG (WR) configuration

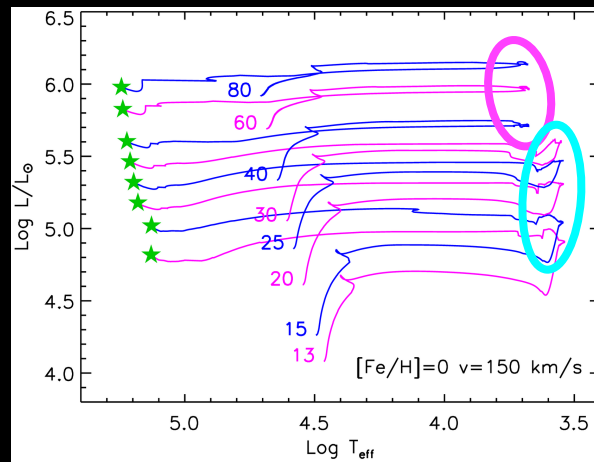
# Core He Depletion: Solar Metallicity Models

## Configuration @ He depletion

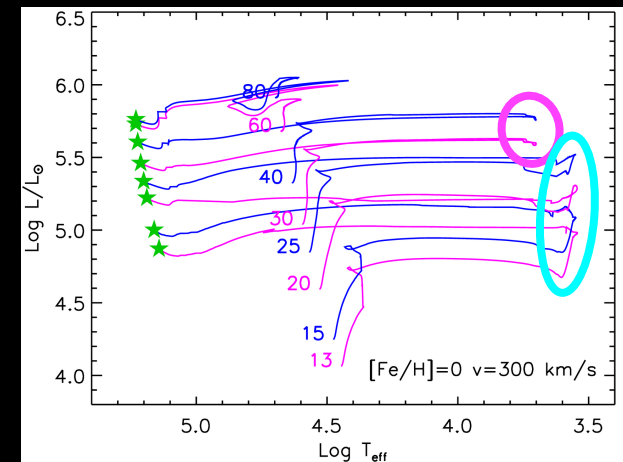
Rotating models are more luminous and cooler  $\rightarrow$  Eddington limit and dust production favored



$v=0$  km/s



$v=150$  km/s



$v=300$  km/s



Stars that reach the Eddington limit



Stars entering the dust production in an early stage of core He burning  $\rightarrow$  becomes BSG/WR stars

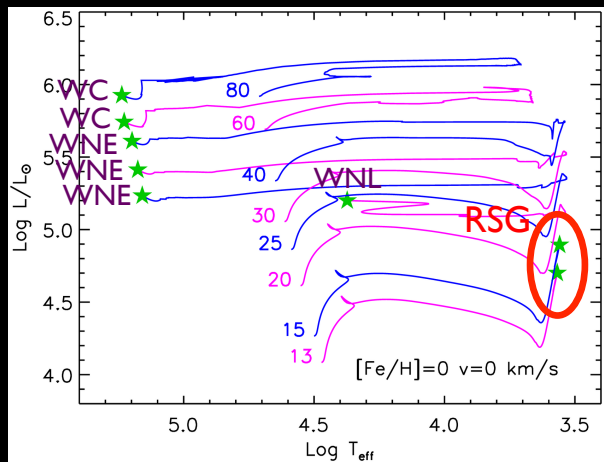


Stars entering the dust production in a late stage of core He burning  $\rightarrow$  remains RSG

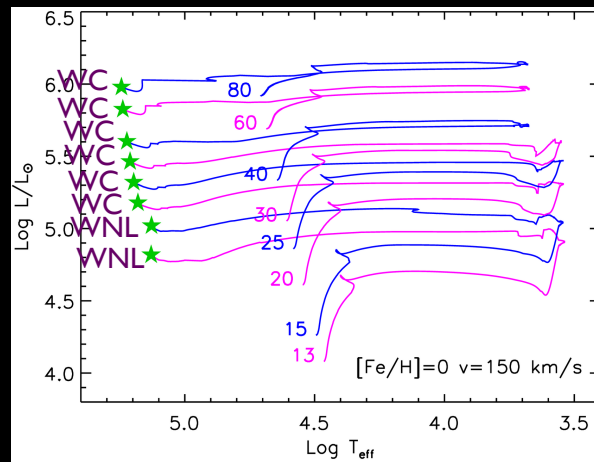
# Core He Depletion: Solar Metallicity Models

## Configuration @ He depletion

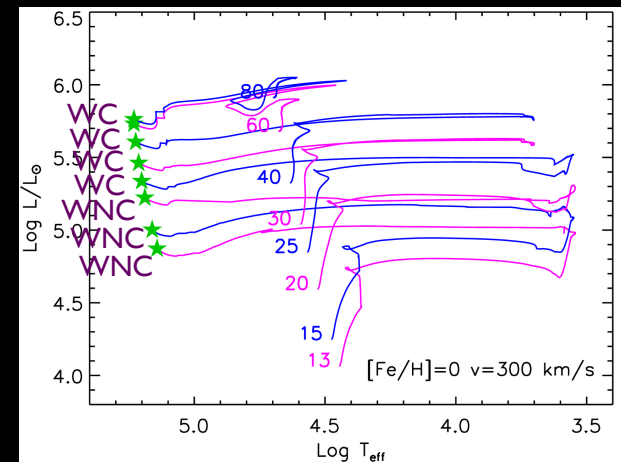
$v=0$  km/s



$v=150$  km/s



$v=300$  km/s



$M \geq 20 M_{\odot}$



WR

$M \geq 13 M_{\odot}$



WR

$M \geq 13 M_{\odot}$



WR

$M \leq 15 M_{\odot}$

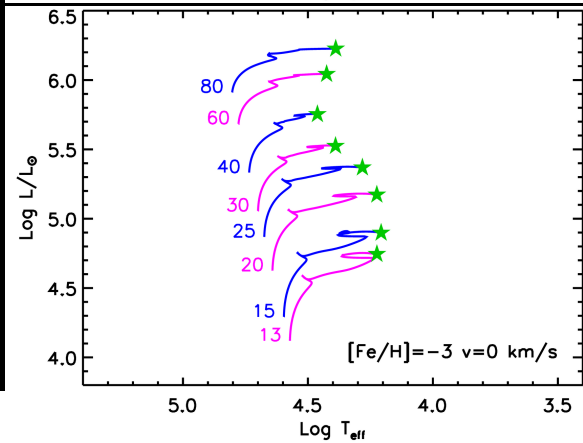
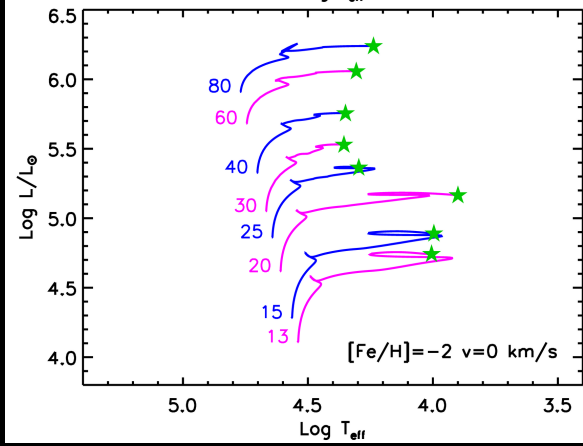
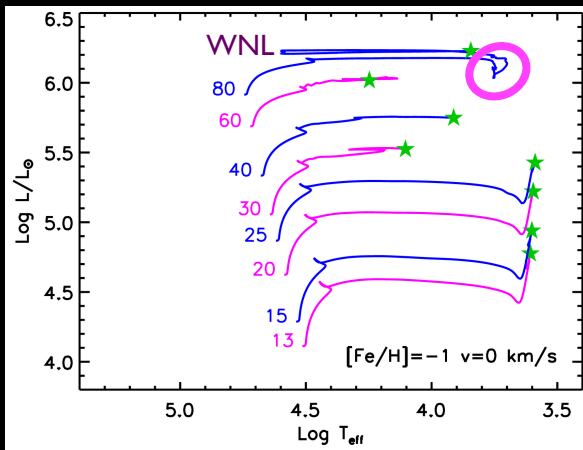


RSG

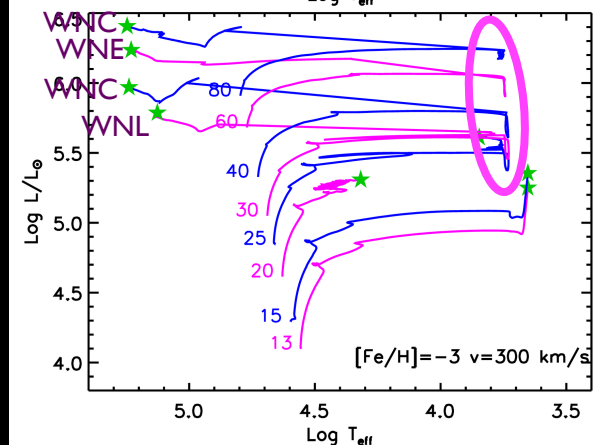
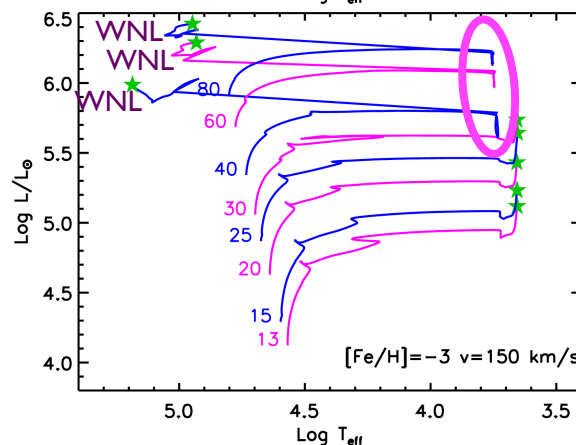
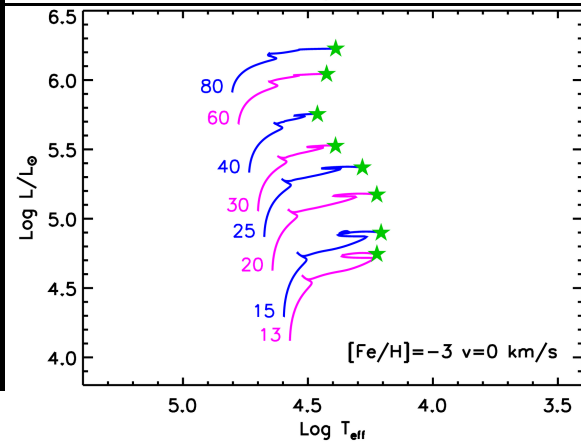
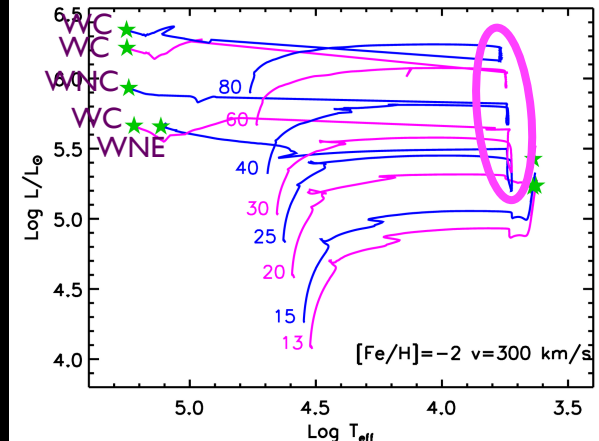
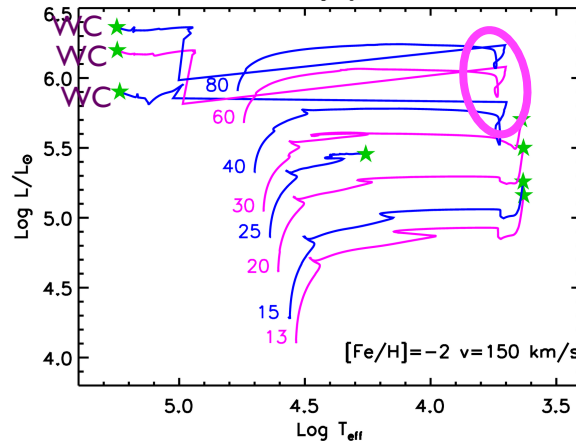
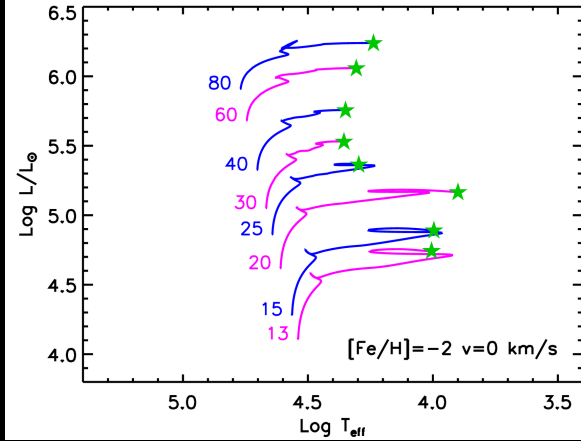
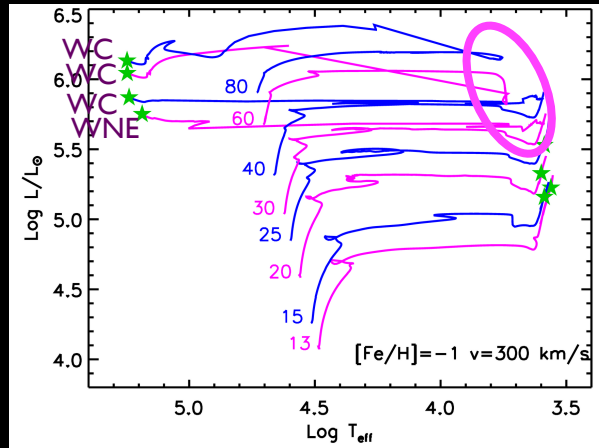
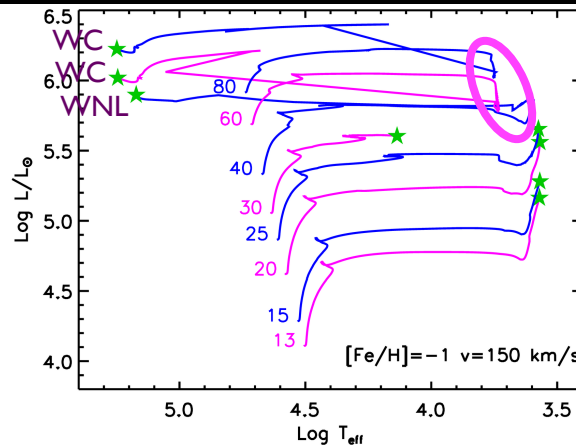
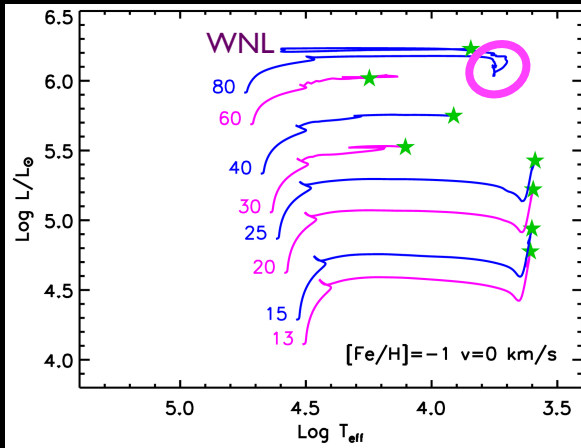
WR :  $\text{Log}_{10}(T_{\text{eff}}) > 4.0$

- WNL:  $10^{-5} < H_{\text{sup}} < 0.4$  (H burning, CNO, products)
- WNE:  $H_{\text{sup}} < 10^{-5}$  (No H)
- WNC:  $0.1 < X(\text{C})/X(\text{N}) < 10$  (both H and He burning products, N and C)
- WC:  $[X(\text{C})+X(\text{O})]/X(\text{He}) < 1$  (He burning products)
- WO:  $[X(\text{C})+X(\text{O})]/X(\text{He}) \geq 1$  (He burning products)

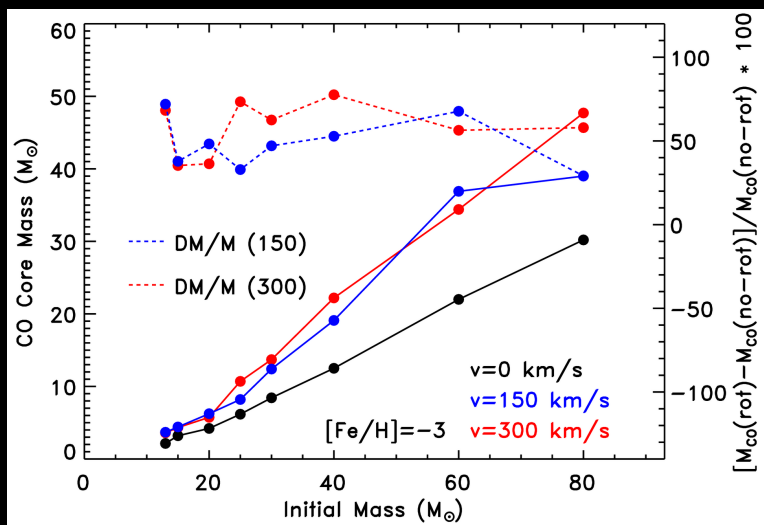
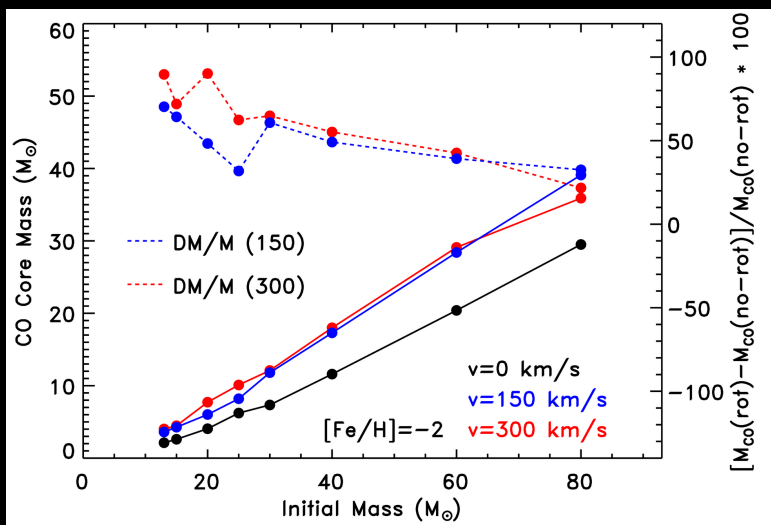
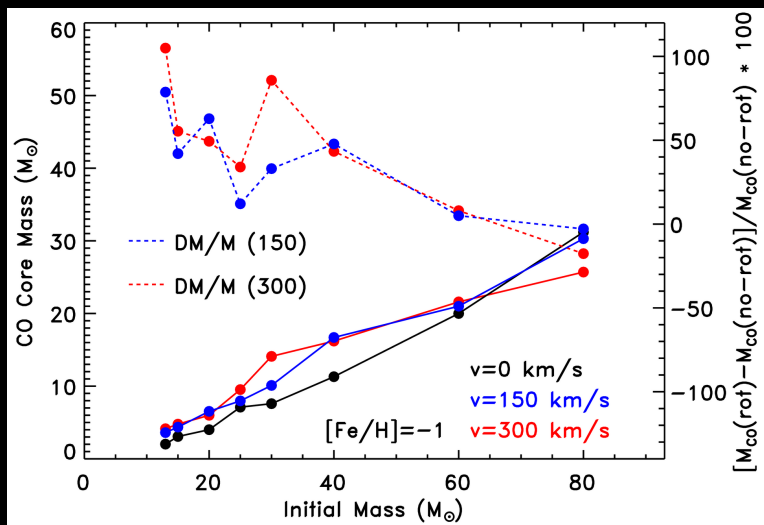
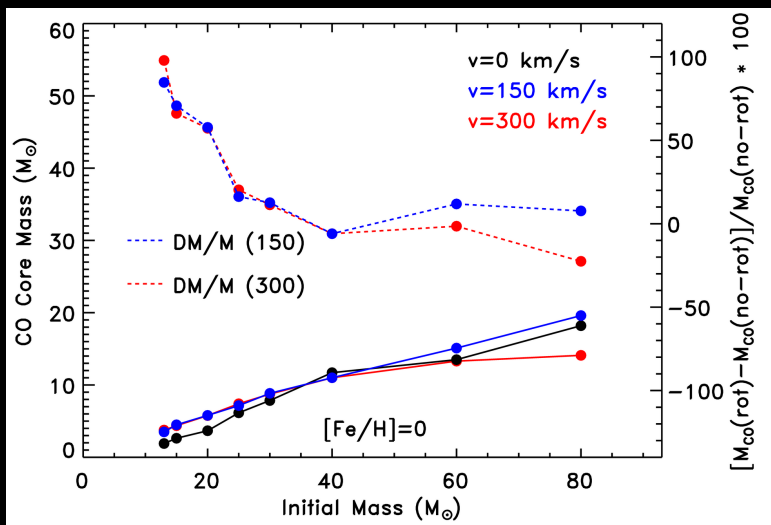
# Core He Depletion: Low Metallicity Models



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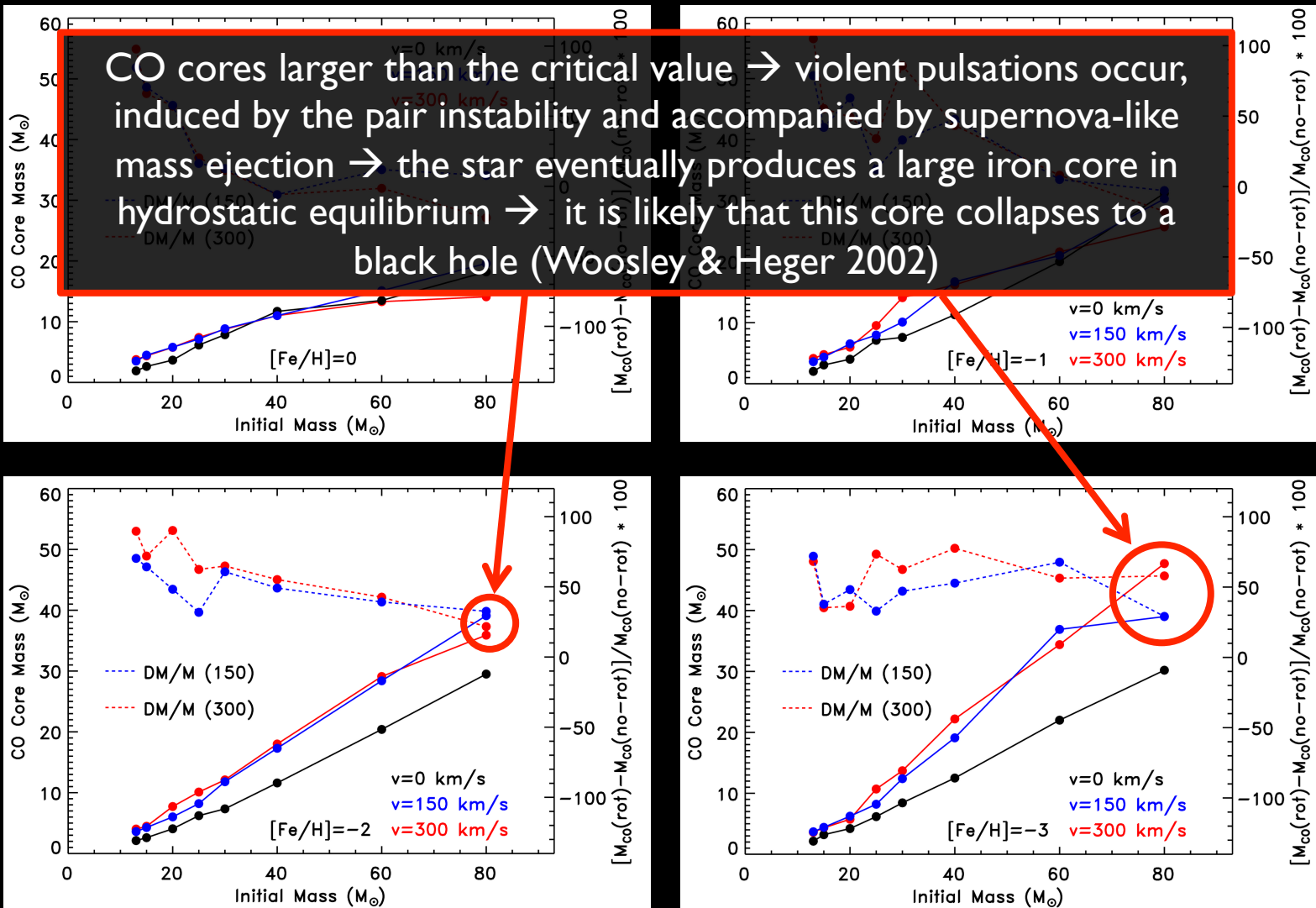
# CO Core Mass @ Core He Depletion



The CO core increases with increasing the initial velocity and with decreasing the metallicity



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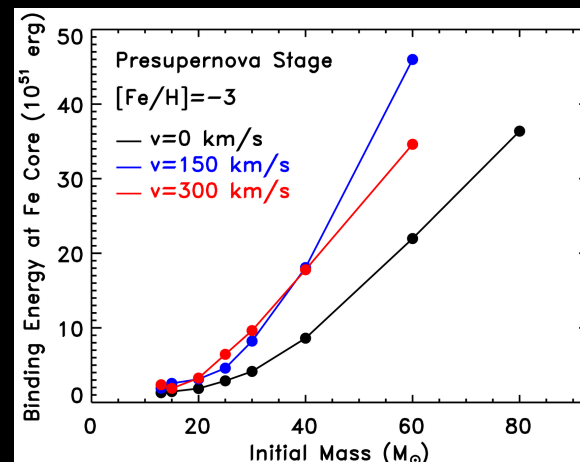
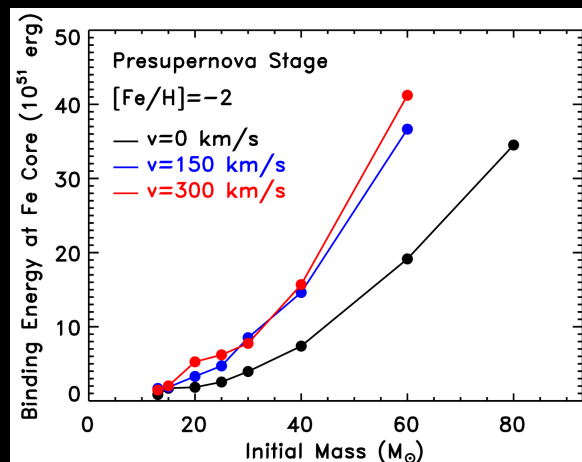
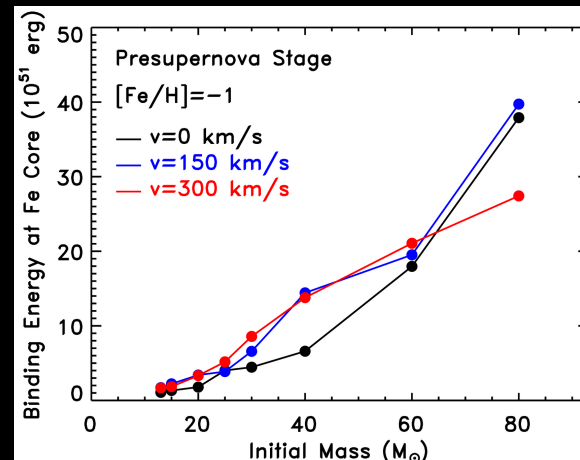
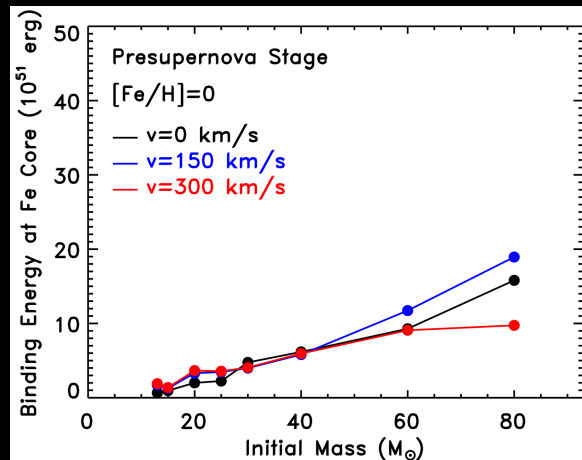
## Advanced Burning Stages

Larger CO at core He depletion



Stronger contraction of the CO core

Presupernova rotating models ( $M < 40 M_{\odot}$ ) appear much more compact compared to the non rotating ones, with larger Fe cores and larger binding energies



We expect larger remnant masses for lower metallicity rotating models

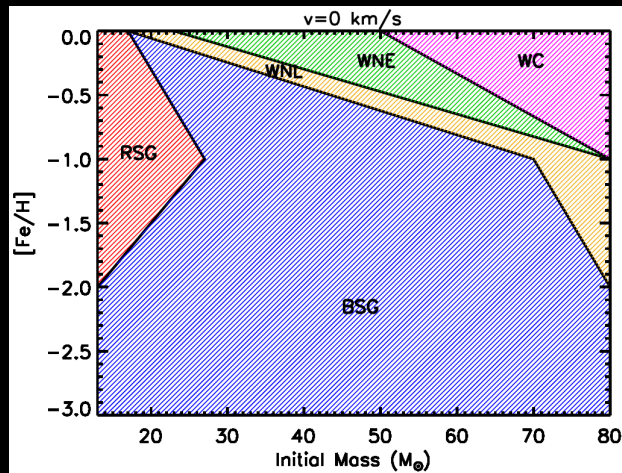
## Configuration @ PreSN Stage

Due to the dramatic speed up of the advanced evolutionary stages the **location of the star in the HR diagram does not change** significantly during these phases

**RSG** = Red Supergiant (extended) SN Progenitor

**BSG** = Blue Supergiant (compact) SN Progenitor

**WX** = Wolf-Rayet (compact) SN Progenitor with no or very little H



Non Rotating Models: the decrease of Mass Loss with metallicity implies:

- RSG progenitors increase down to  $[Fe/H]=-1$  and then disappears below  $[Fe/H]=-2$
- WR progenitors progressively decrease and disappears below  $[Fe/H]=-2$

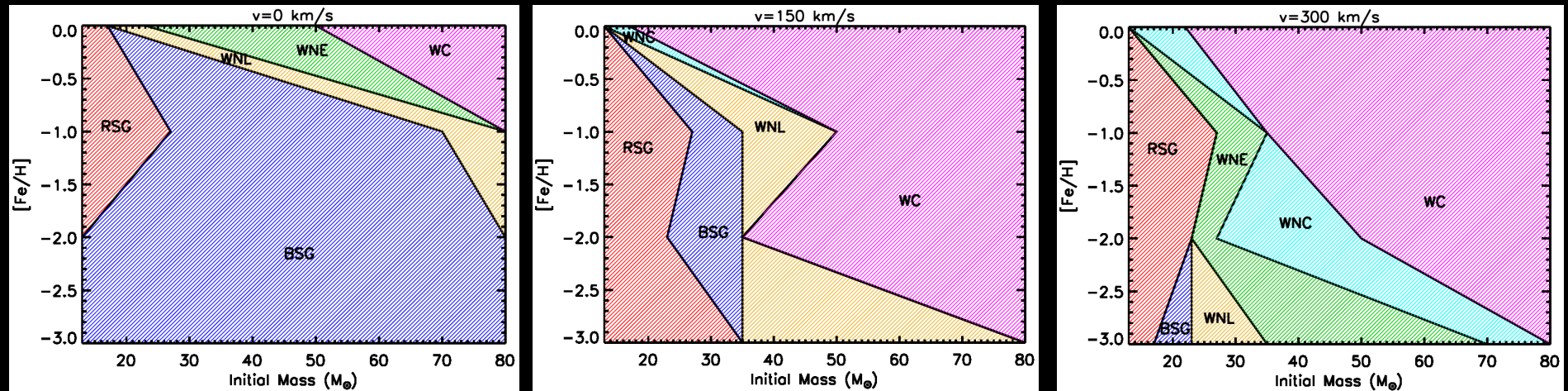
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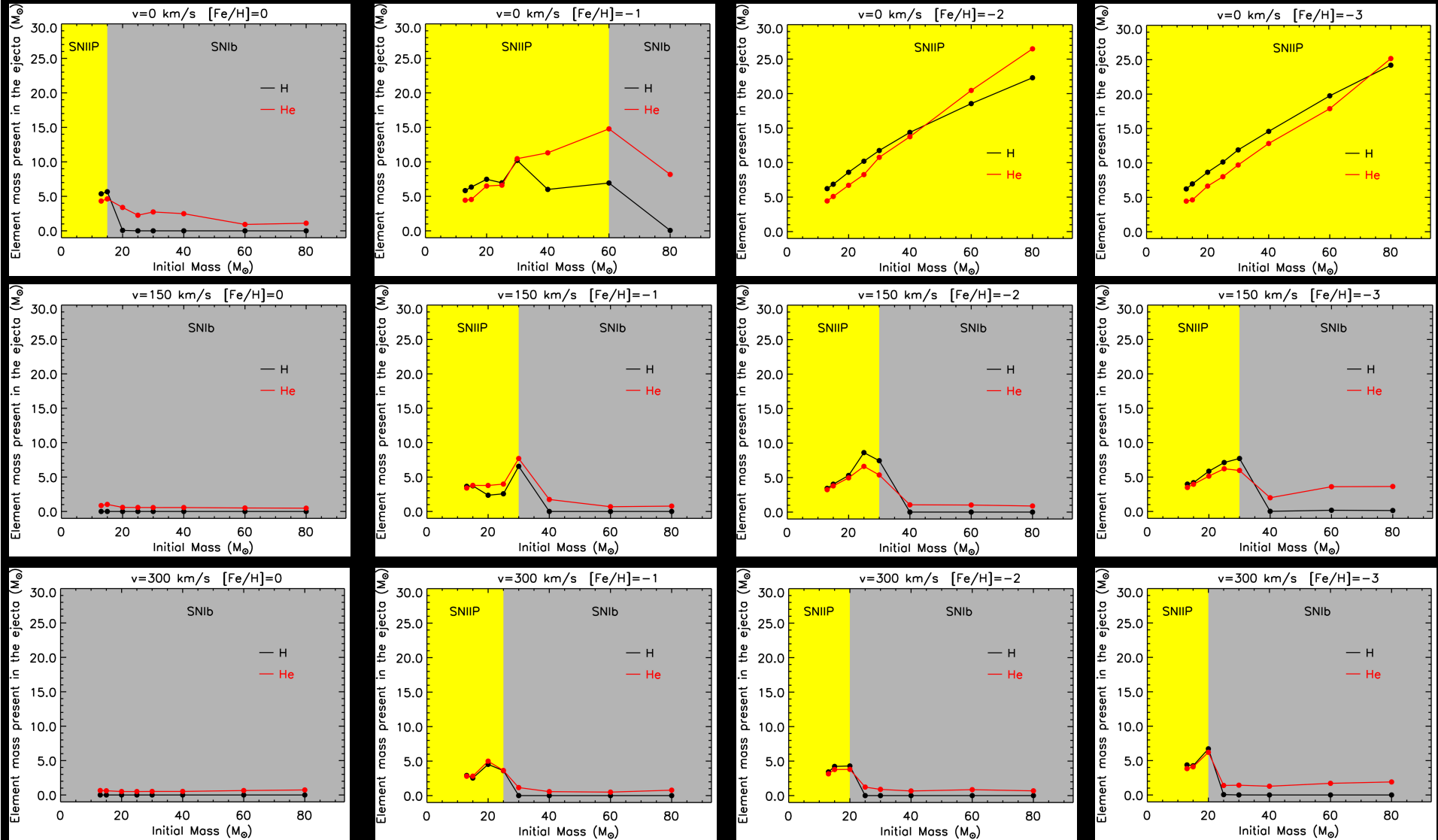
- RSG progenitors increase down to  $[Fe/H]=-1$  and then disappears below  $[Fe/H]=-2$
- WR progenitors progressively decrease and disappears below  $[Fe/H]=-2$

Rotating Models: the inclusion of rotation **reduces the minimum mass entering the WR phase and increases the maximum mass becoming RSG @ all metallicities**

- RSG progenitors increase at lower metallicities (reduction of effective gravity)
- WR progenitors increase at lower metallicities (direct/indirect enhancement of mass loss)

# The Final Fate: SN Types

Limiting H/He masses for the formation of the various SNe from Hachinger+ 2012



- Increasing fraction of SNIIP with decreasing  $[Fe/H]$  and with decreasing  $v$
- No SNIc predicted for any  $[Fe/H]$  and  $v$

# INDUCED EXPLOSION, EXPLOSIVE NUCLEOSYNTHESIS AND FALLBACK

Propagation of the shock wave followed by means of an explosive simulation code, developed by us, that solves the fully compressible reactive hydrodynamic equations using the piecewise parabolic method ( PPM - Colella & Woodward 1984) in the Lagrangean form

Chemical evolution of the matter computed by coupling the same nuclear network adopted in the hydrostatic calculations to the system of hydrodynamic equations.

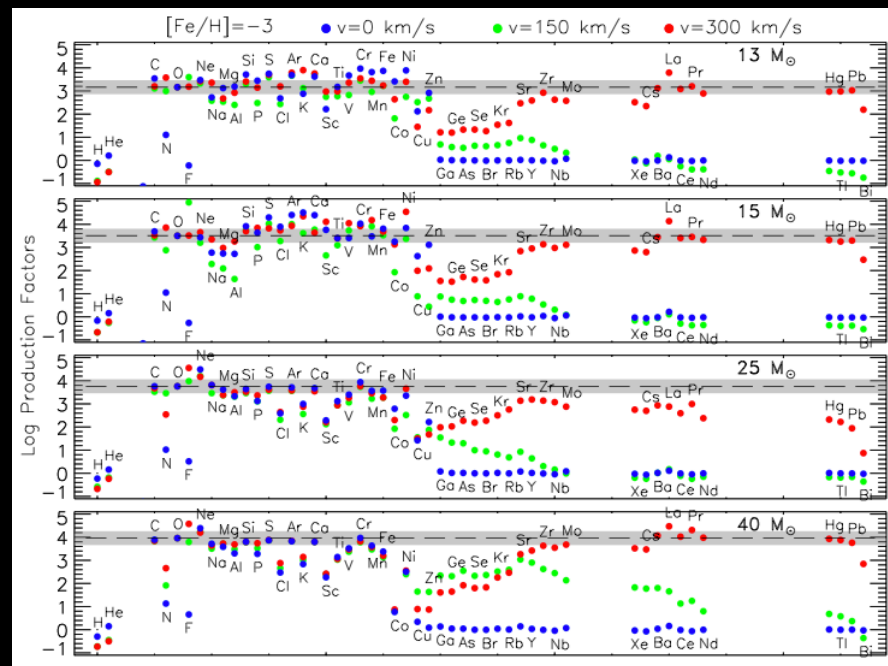
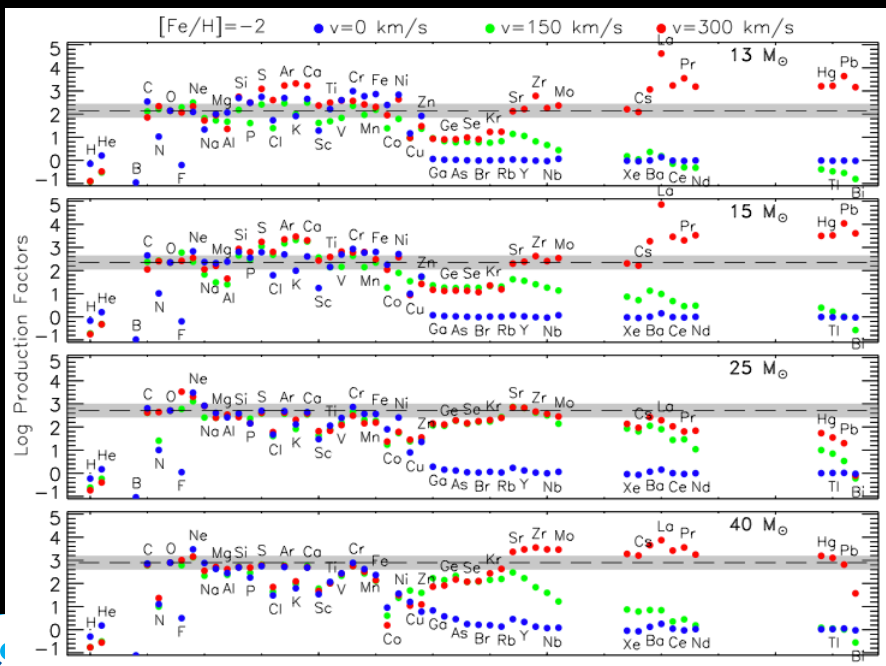
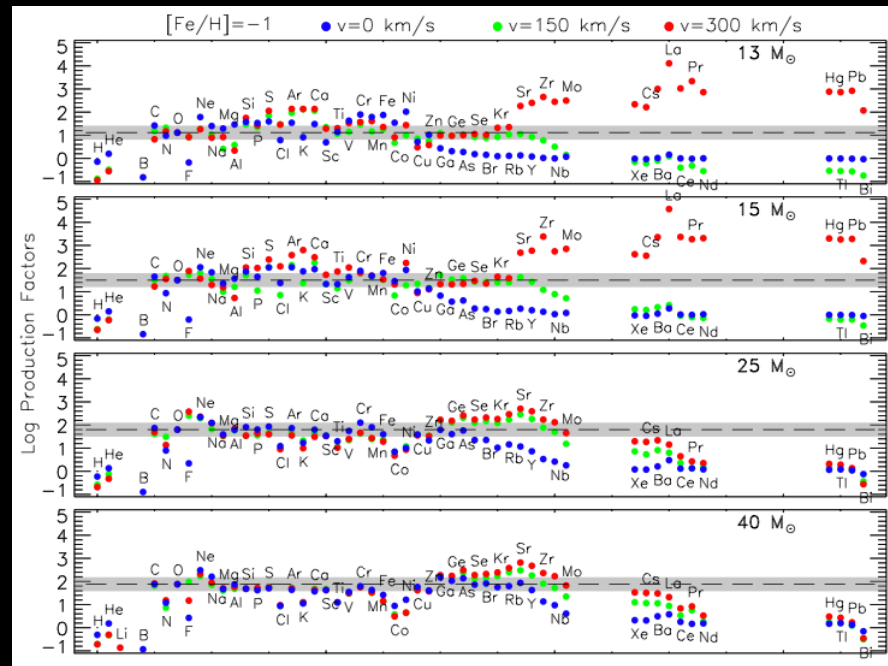
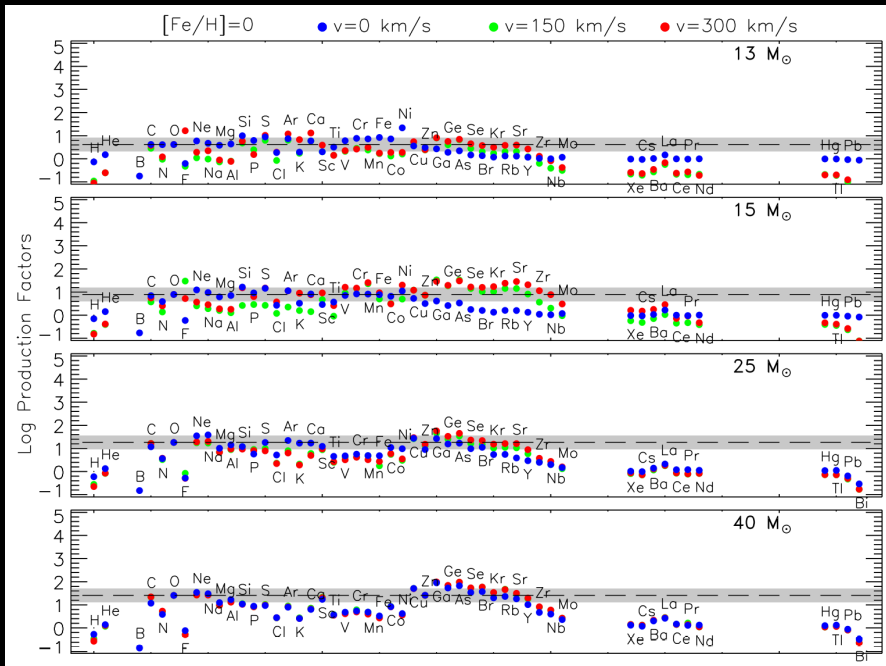
$$\frac{\partial v}{\partial t} = -\frac{Gm}{r^2} - 4\pi r^2 \frac{\partial P}{\partial m}$$

$$\frac{\partial r}{\partial m} = \frac{1}{4\pi r^2 \rho}$$

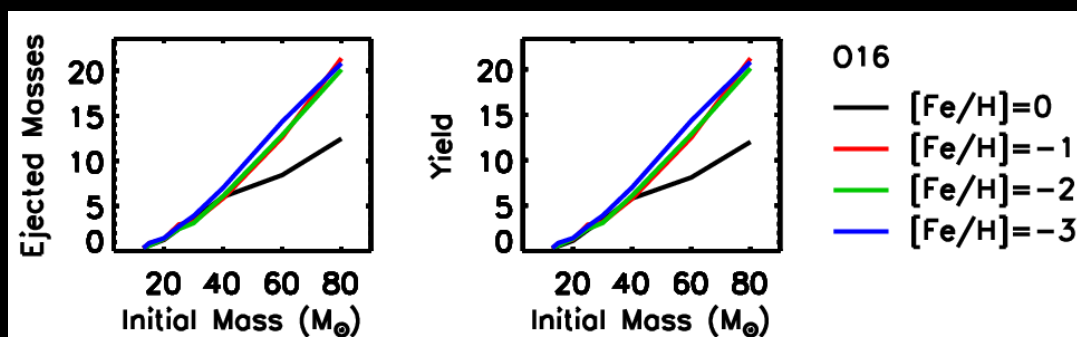
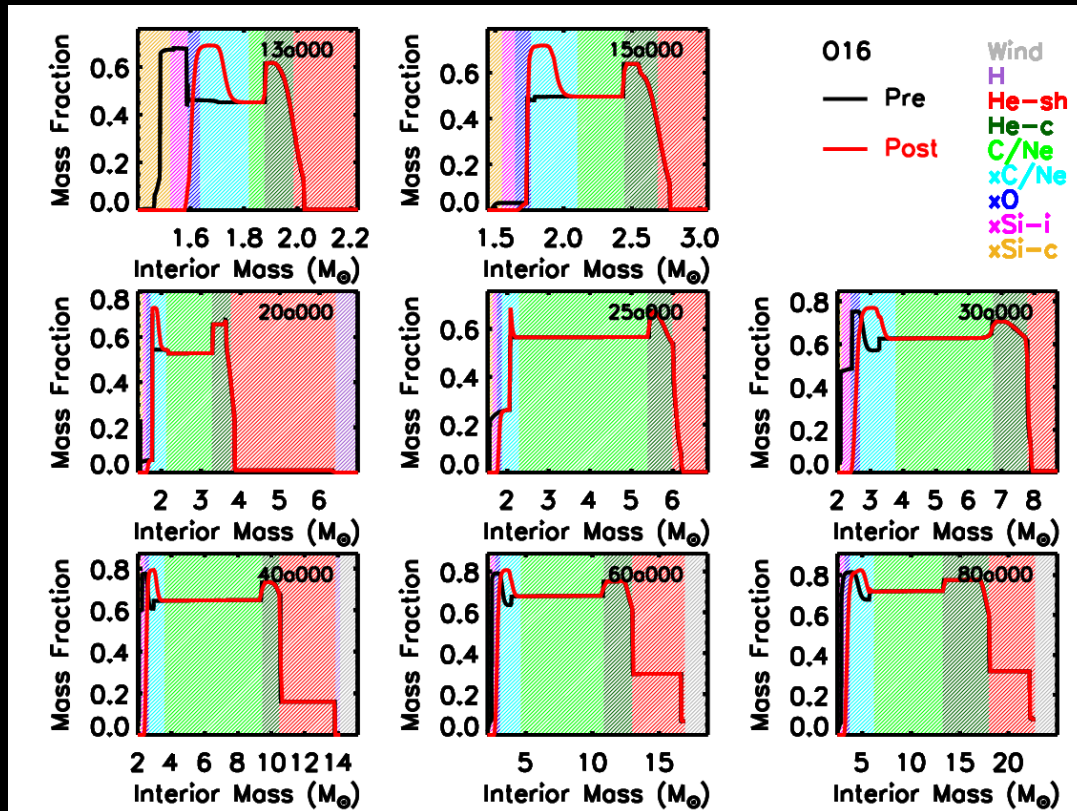
$$\frac{\partial e}{\partial t} = \frac{P}{\rho^2} \frac{\partial \rho}{\partial t}$$

$$\begin{aligned} \frac{\partial Y_i}{\partial t} = & \sum_j c_i(j) \lambda_j Y_j + \sum_{j,k} c_i(j,k) \rho N_A \langle \sigma v \rangle_{j,k} Y_j Y_k \\ & + \sum_{j,k,l} c_i(j,k,l) \rho^2 N_A^2 \langle \sigma v \rangle_{j,k,l} Y_j Y_k Y_l \quad i = 1, \dots, N \end{aligned}$$

# Chemical Yields @ Various Metallicities and Initial Velocities



# The $\alpha$ -elements O Mg Si Ca: Non Rotating Models



Most abundant isotope:  $^{16}\text{O}$

Production Site: Hydrostatic He burning

N.B. In the less massive stars the hydrostatic production is partially modified by the explosion

Although  $^{16}\text{O}$  maybe considered as a “hydrostatic” isotope a reliable value of its yield requires the computation of the explosive nucleosynthesis

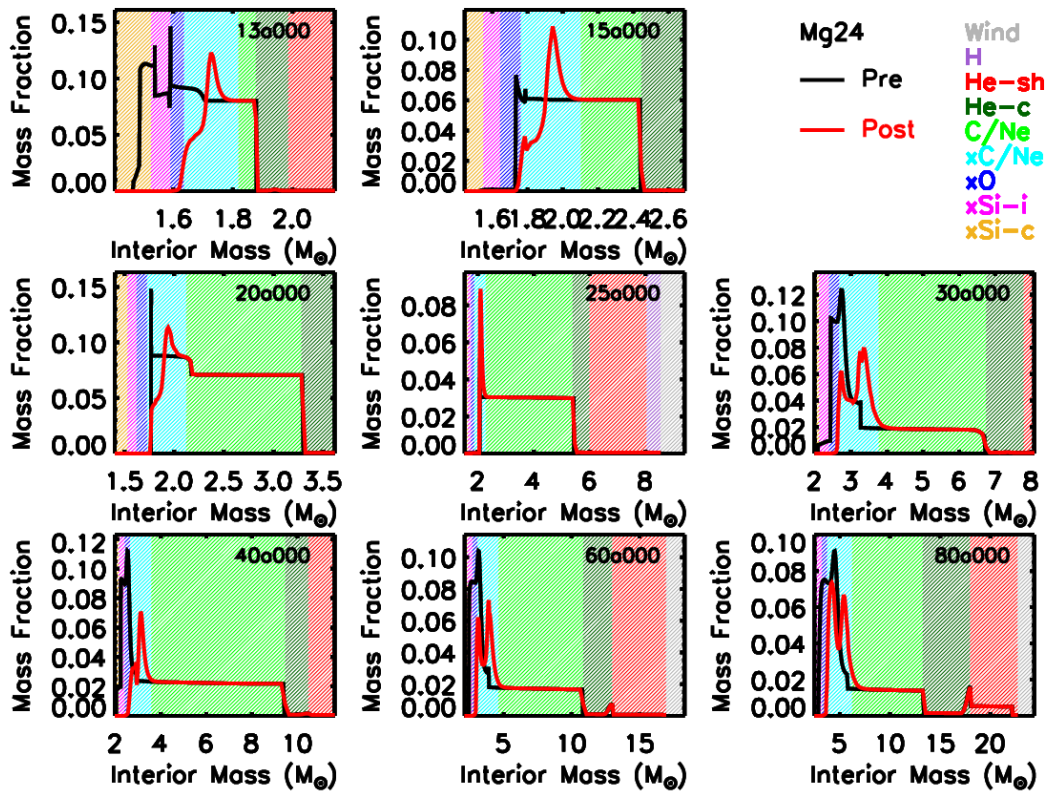
Produced by massive stars

Follows the same trend of the He Core Mass vs Initial Mass

Mild dependence on metallicity with the exception of the most massive solar metallicity stars (mass loss reduces the He core)



# The $\alpha$ -elements O Mg Si Ca: Non Rotating Models

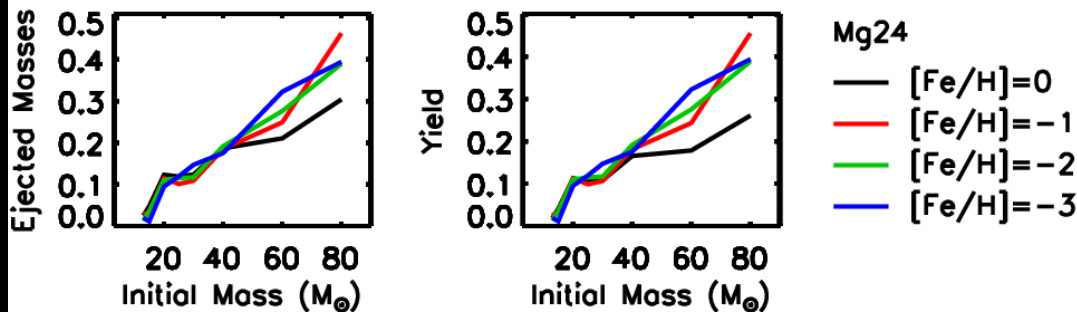


Most abundant isotope:  $^{24}\text{Mg}$

Production Site: Hydrostatic C/Ne burn.

N.B. In the less massive stars the hydrostatic production is even substantially modified by the explosion

Although  $^{24}\text{Mg}$  maybe considered as a “hydrostatic” isotope a reliable value of its yield requires the computation of the explosive nucleosynthesis

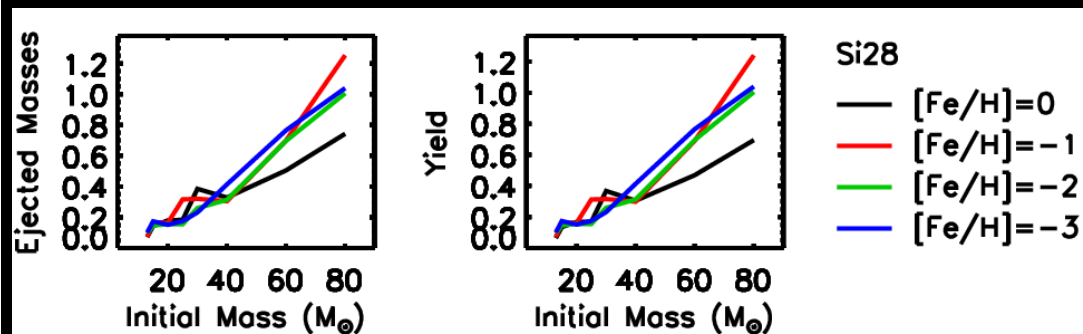
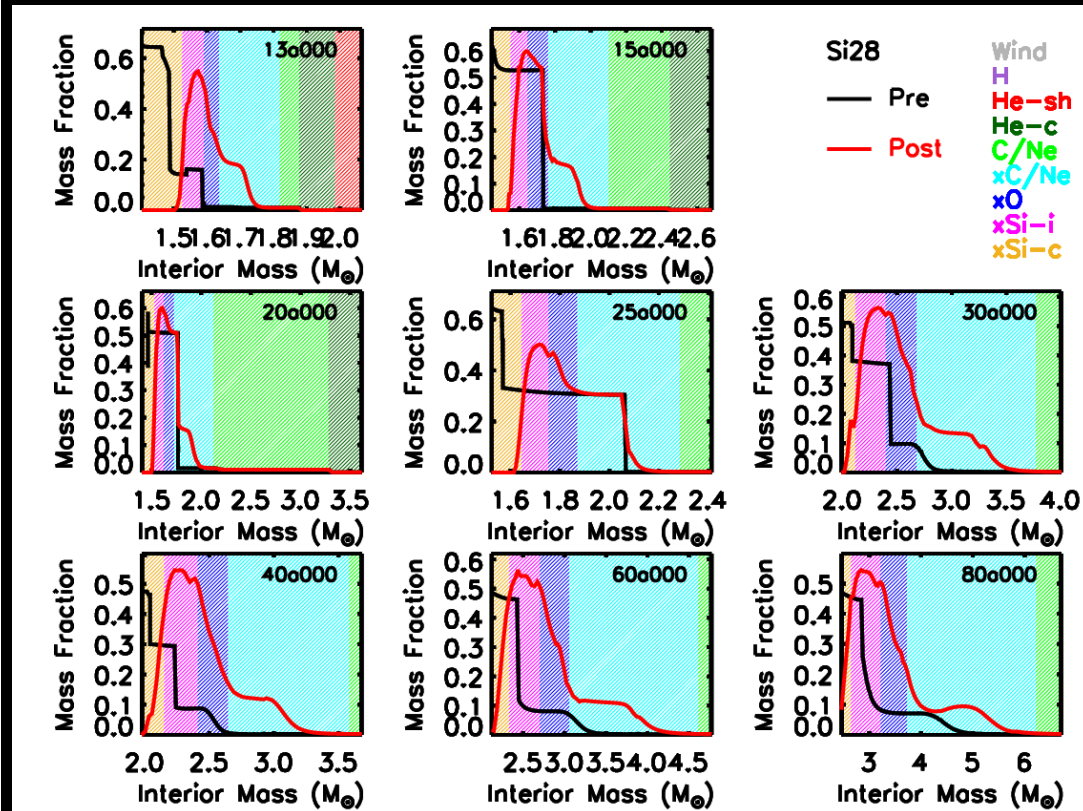


Produced by massive stars

Follows the same trend of the C/Ne shell Mass vs Initial Mass

Non monothonic dependence on metallicity increasing for massive stars ( $M \geq 40 M_{\odot}$ )

# The $\alpha$ -elements O Mg Si Ca: Non Rotating Models



Most abundant isotope:  $^{28}\text{Si}$

Production Site: Hyd. O – Expl. Si-i –  
Expl. O – Expl. C/Ne

N.B. The relative proportions vary from star to star

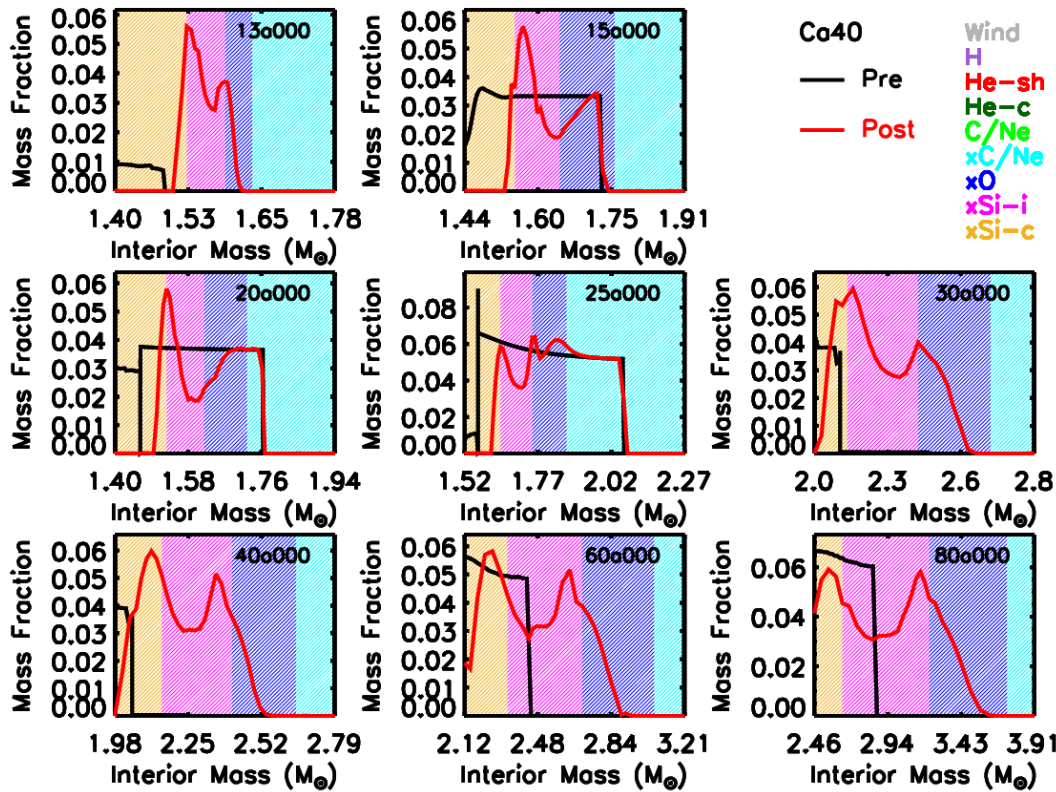
The computation of the yield of  $^{28}\text{Si}$  necessarily requires the computation of the explosive nucleosynthesis

Produced by massive stars

Increases with the initial mass (on average)

Non monothonic dependence on metallicity. Larger variations for the most massive stars ( $M \geq 40 M_{\odot}$ )

# The $\alpha$ -elements O Mg Si Ca: Non Rotating Models

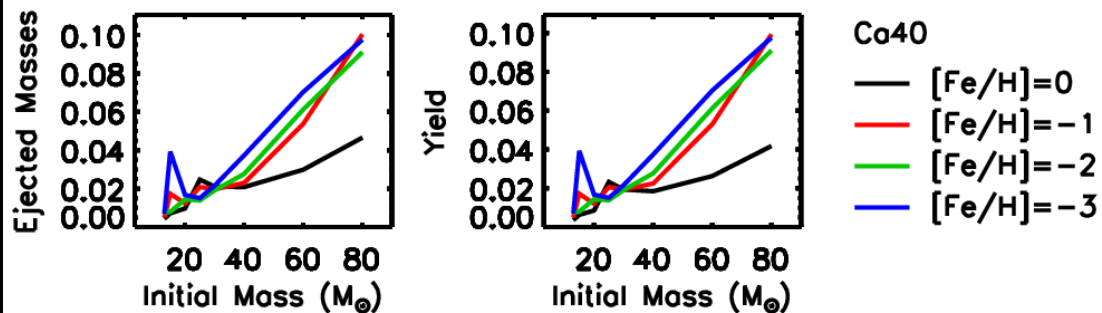


Most abundant isotope:  $^{40}\text{Ca}$

Production Site: Hyd. O – Expl. Si-C –  
Expl. Si-i – Expl. O

N.B. The relative proportions vary  
from star to star

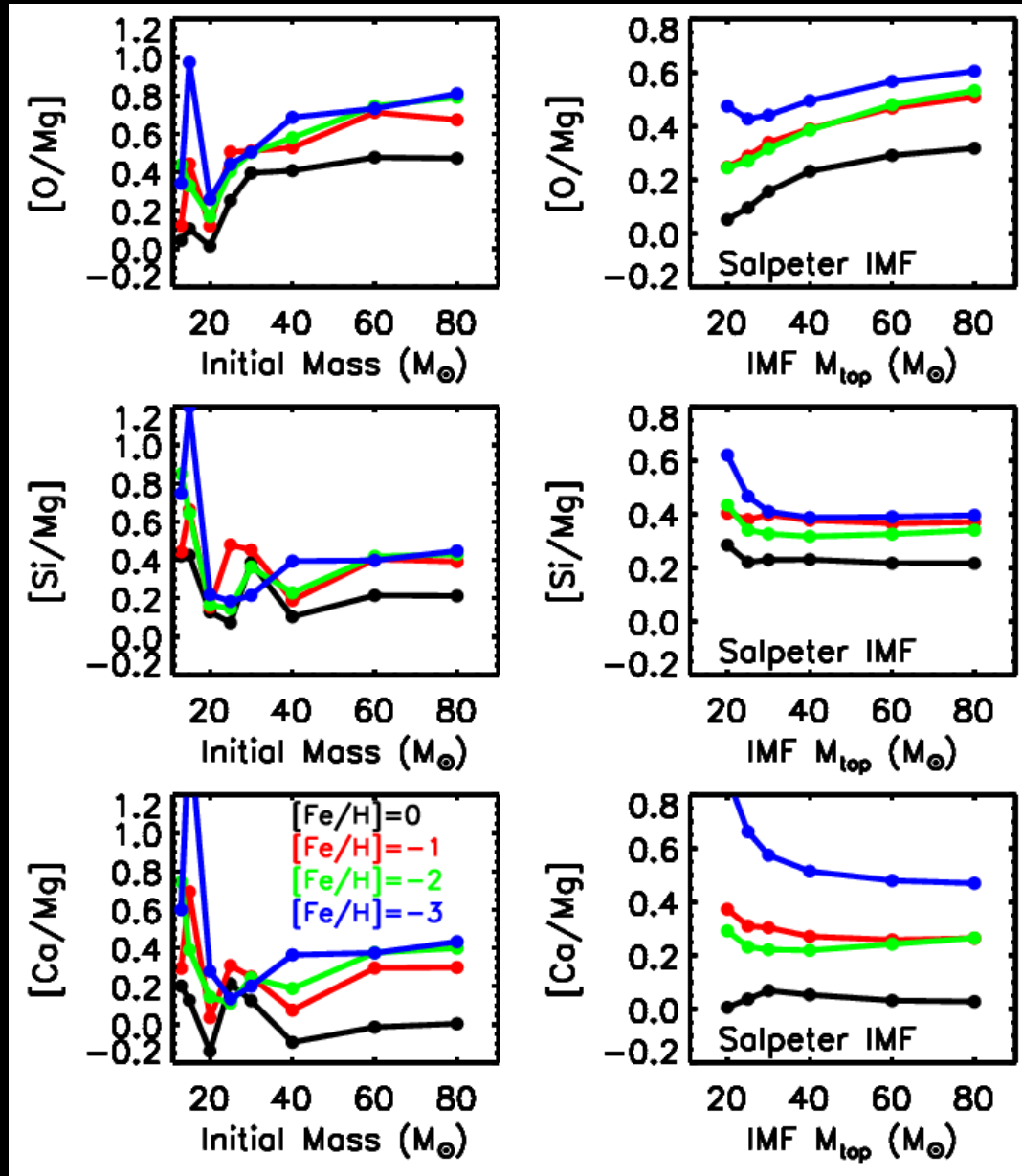
The computation of the yield of  $^{40}\text{Ca}$   
necessarily requires the computation  
of the explosive nucleosynthesis



Produced by massive stars

On average it increases with  
the mass and decreases with  
the metallicity although the  
behavior is not always  
monothonic

## The $\alpha$ -elements O Mg Si Ca: Non Rotating Models



Increases on average with the mass and decreases with the increasing the metallicity

The most massive stars play a role

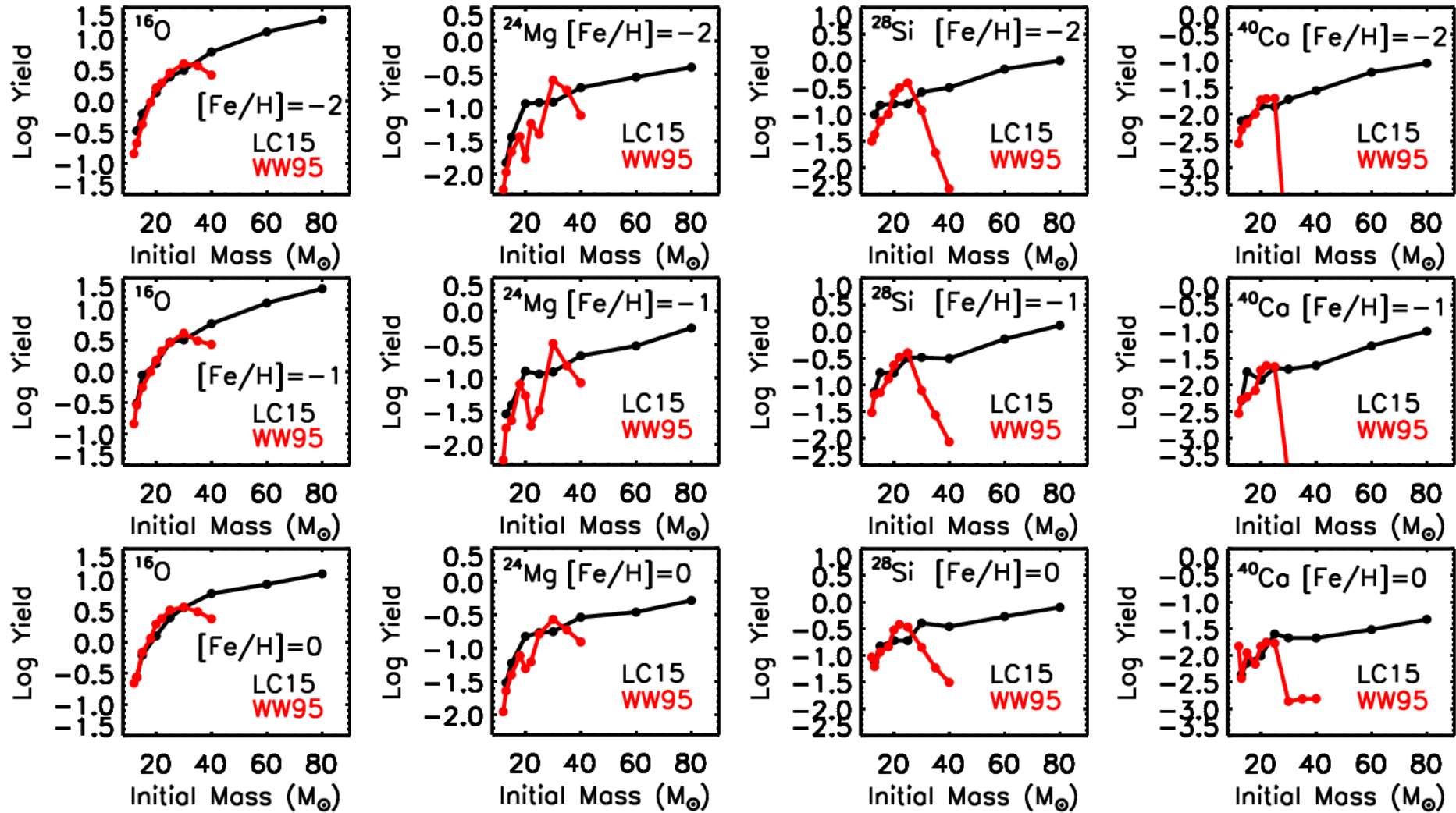
Decrease on average with the mass up to  $M \sim 40 M_{\odot}$ . For higher masses they are almost constant.

They decrease with the increasing the metallicity

The most massive stars does not change substantially  $[Si, Ca/Mg]$

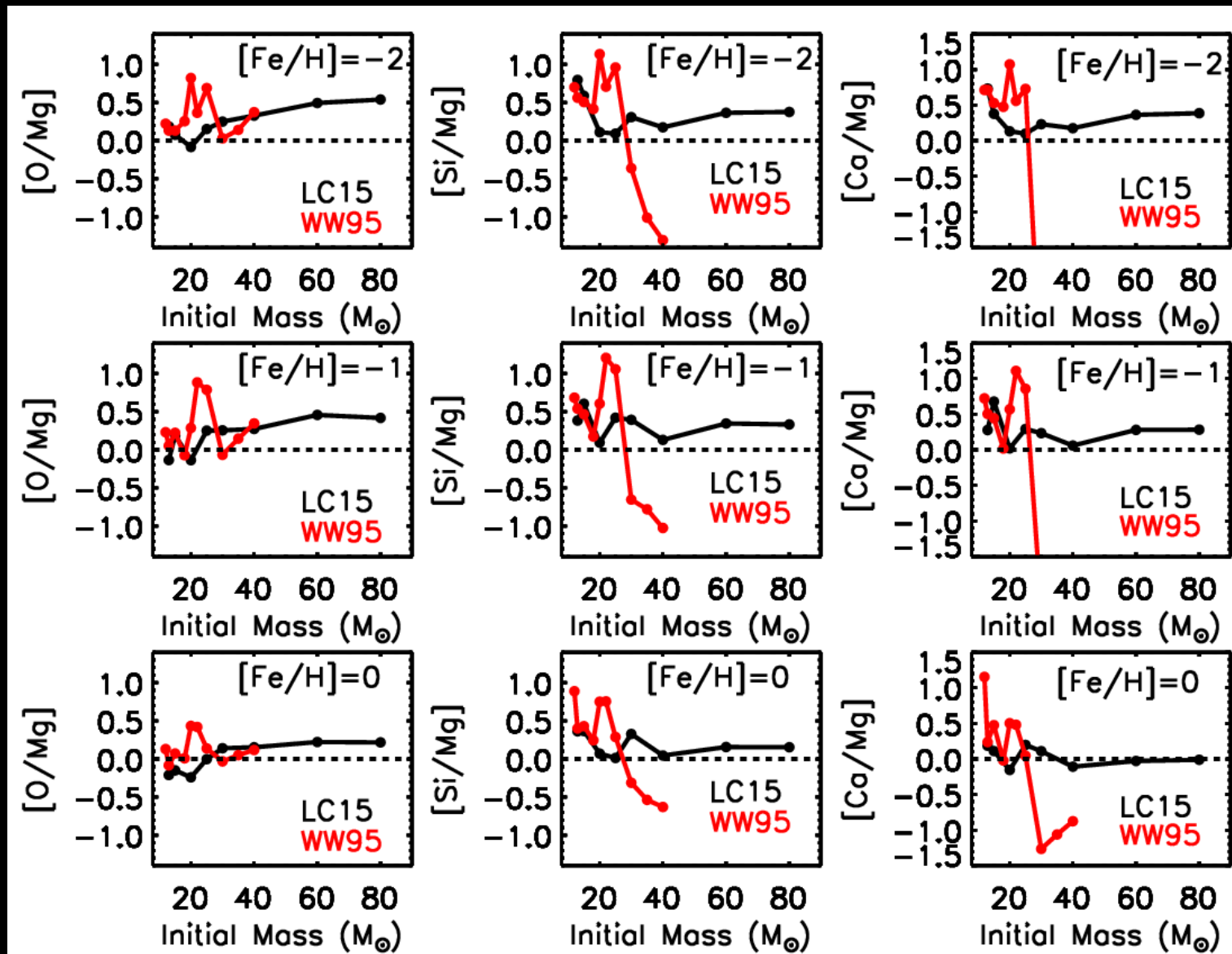
# The $\alpha$ -elements O Mg Si Ca: Non Rotating Models

## Comparison with Woosley & Weaver 1995 (WW95)



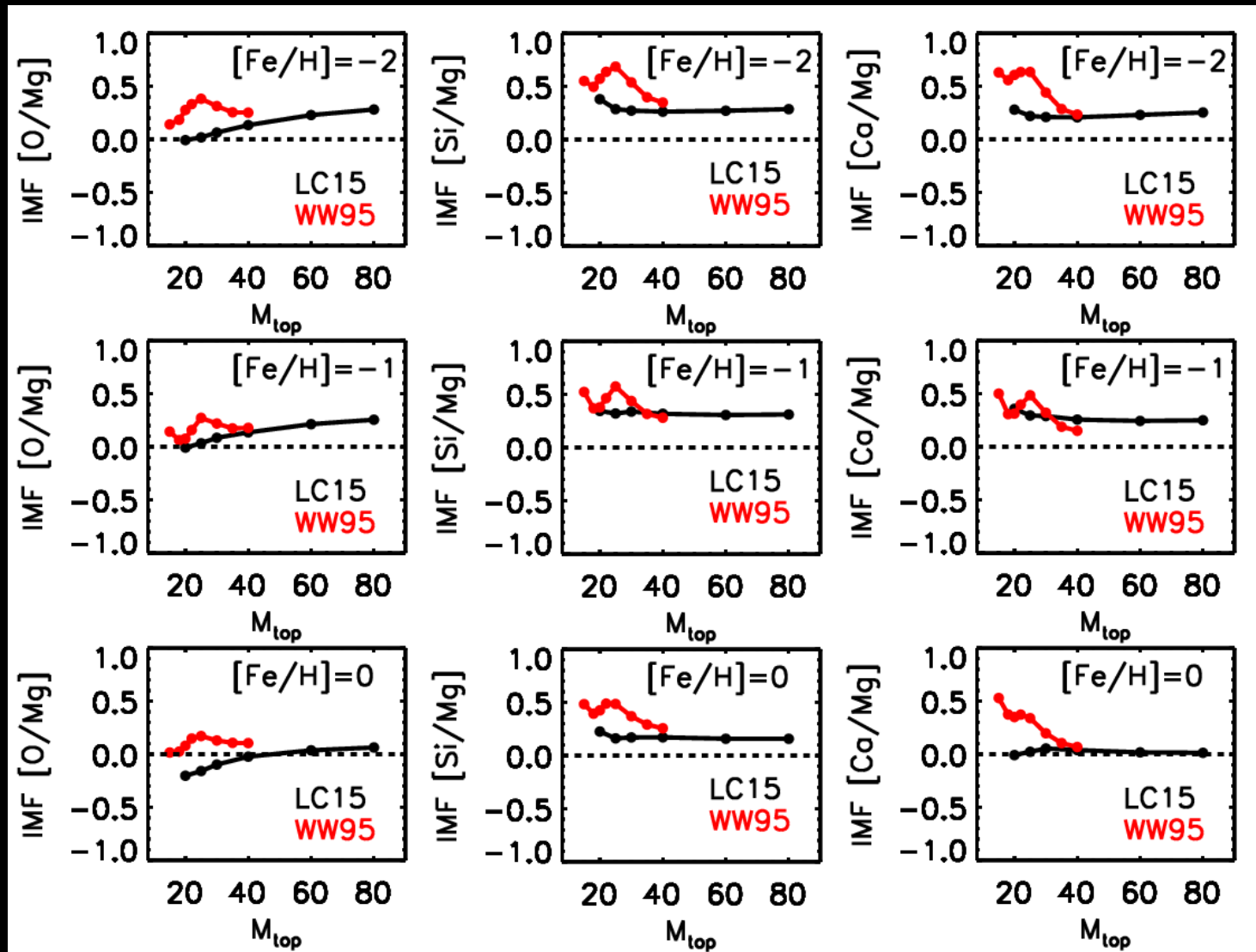
# The $\alpha$ -elements O Mg Si Ca: Non Rotating Models

## Comparison with Woosley & Weaver 1995 (WW95)

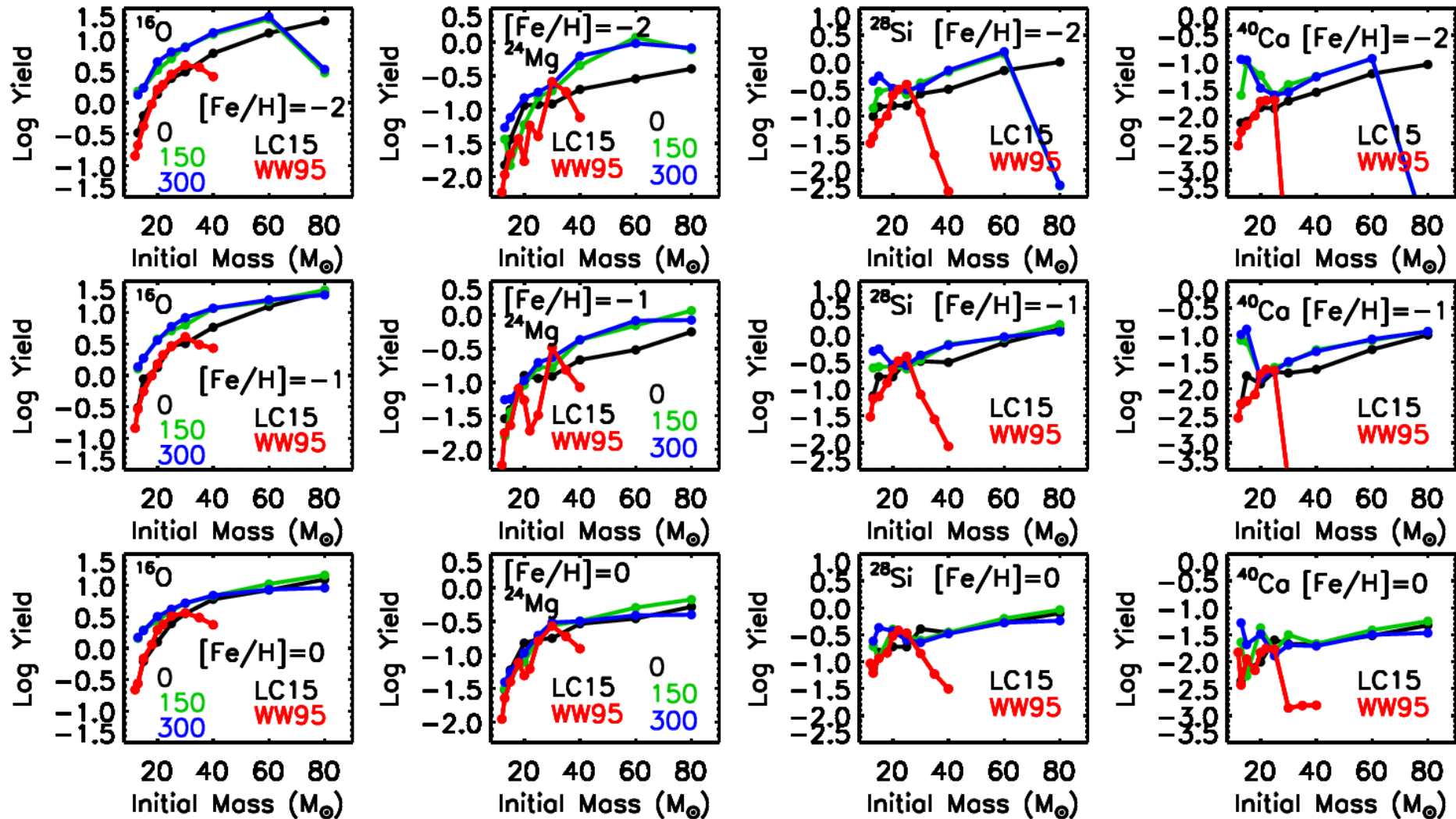


# The $\alpha$ -elements O Mg Si Ca: Non Rotating Models

## Comparison with Woosley & Weaver 1995 (WW95)

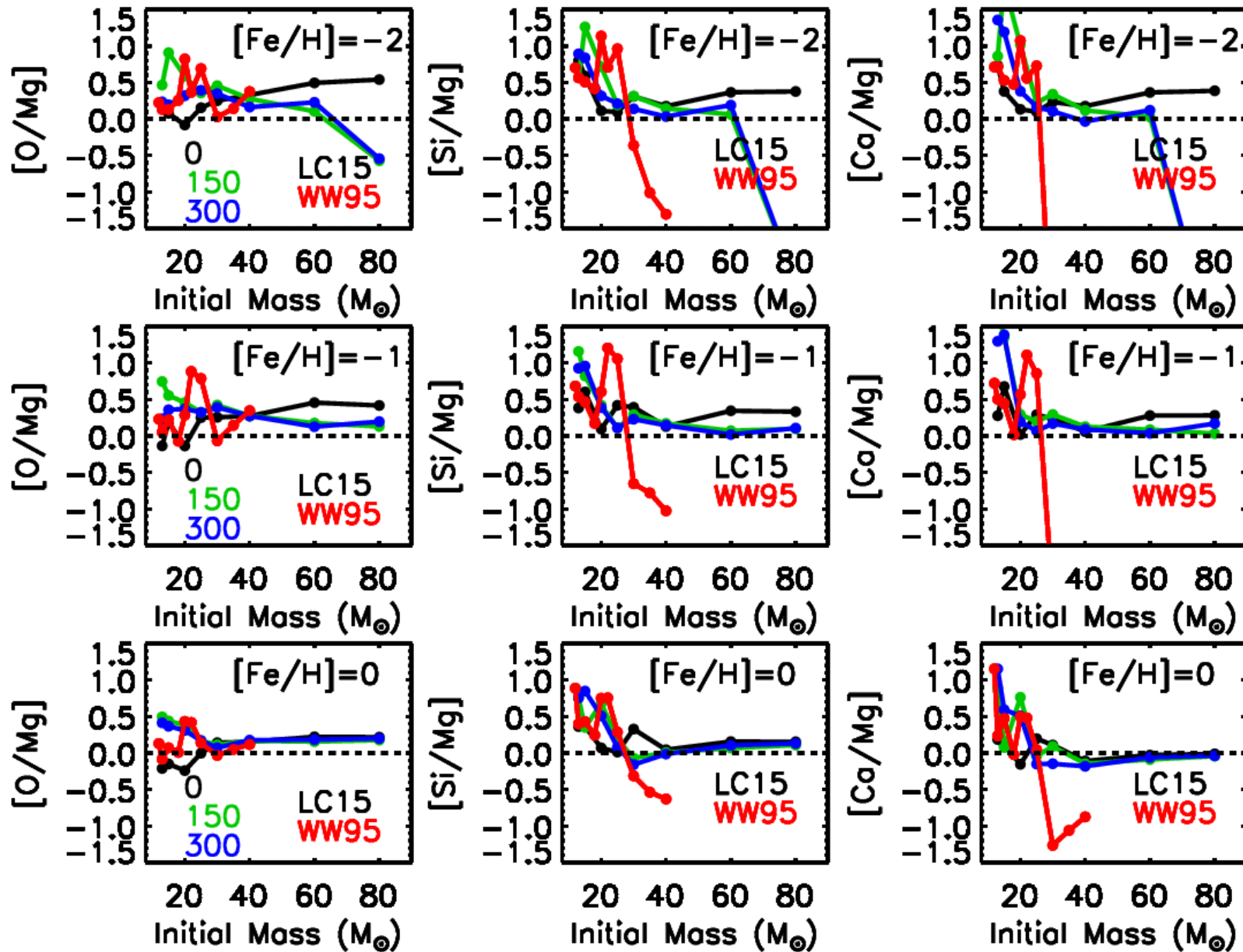


# The $\alpha$ -elements O Mg Si Ca: Effect of Rotation

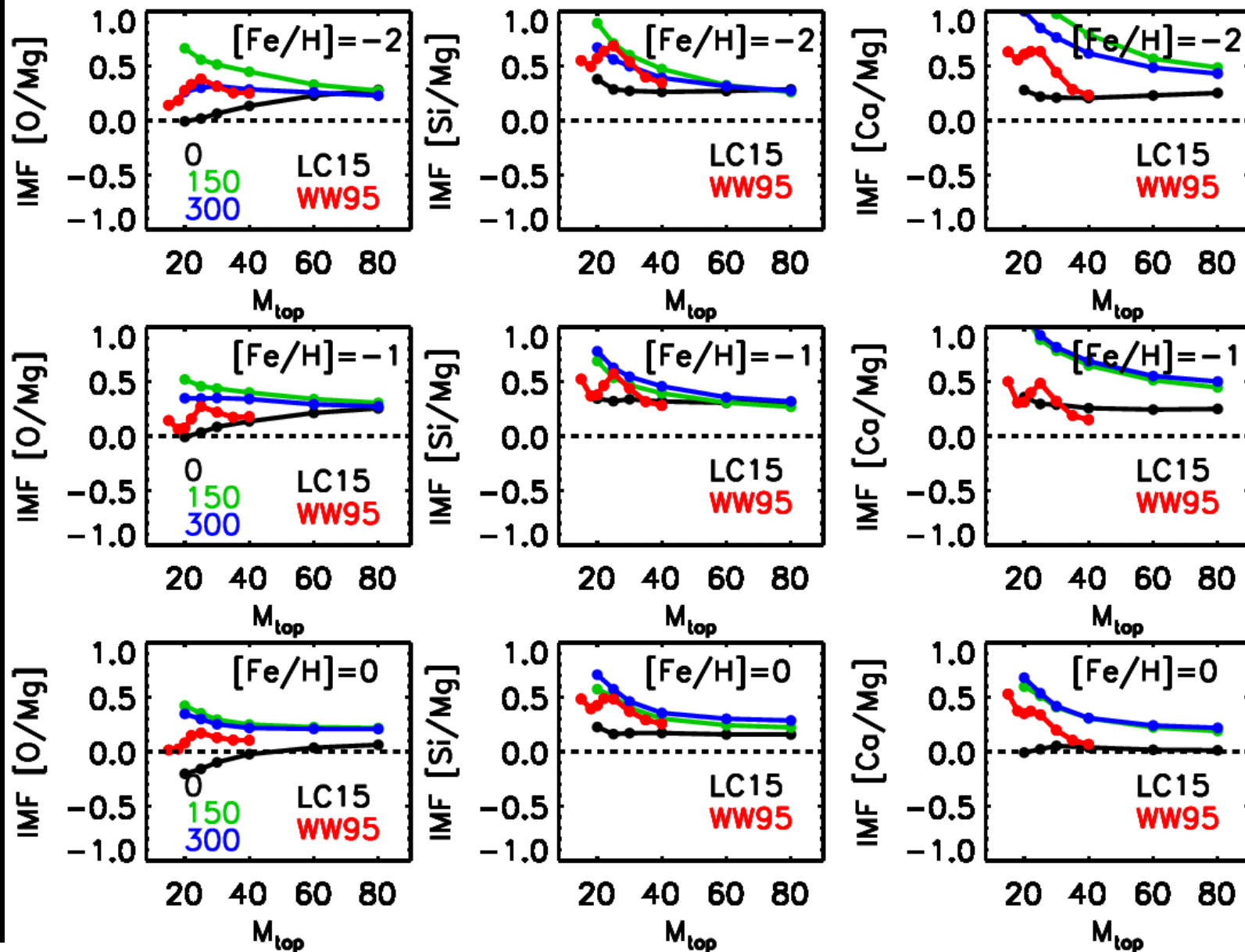




# The $\alpha$ -elements O Mg Si Ca: Effect of Rotation



# The $\alpha$ -elements O Mg Si Ca: Effect of Rotation



## Summary and Conclusions

The inclusion of rotation makes:

- Larger cores (direct effect)
- More efficient mass loss (indirect effect)

The interplay between these two effects lead to:

- More compact structure @ preSN stage → more massive remnants
- Increase of the RSG and WR SN progenitors at all metallicities
- Increase of SNIb/SNII fraction at all metallicities

Nucleosynthesis:

- PFs of the majority of the elements increase with the mass for any fixed metallicity and increase for any fixed mass with decreasing the metallicity
- No production of elements heavier than Zn is obtained in non rotating models for metallicities  $[Fe/H] < -1$
- The inclusion of rotation enhances the production of N, F and all the elements heavier than Zn up to Pb
- This effect is higher for lower metallicities (more efficient rotational mixing) and for lower mass models (higher angular momentum for a fixed initial velocity)

## Summary and Conclusions

[O/Mg], [Si/Mg] and [Ca/Mg] we find:

For non rotating models:

- [O/Mg] decreases with the mass while [Si,Ca/Mg] increase with the mass
- All of them decrease with decreasing the metallicity
- Same behavior is found for the ratios integrated over a IMF
- The inclusion of more massive stars ( $M > 40 M_{\odot}$ ) lead to an increase of the IMF integrated [O/Mg] by about 0.1-0.2 dex. No sizeable variation is found for [Si,Ca/Mg]
- WW95  $^{16}\text{O}$ ,  $^{28}\text{Si}$  and  $^{40}\text{Ca}$  yields are on average lower for lower masses ( $M < 20 M_{\odot}$ ) and larger for larger masses at all metallicities. WW95 models of mass ( $M > 40 M_{\odot}$ ) do not ejected substantial amounts of heavy elements
- WW95  $^{24}\text{Mg}$  is always lower than ours at all metallicities
- A similar behavior is found for the individual ratios
- Our ratios integrated over a IMF up to  $M = 40 M_{\odot}$  are always lower than the corresponding WW95 values ( $\sim 0.1$  dex) or in some cases in agreement
- Integration up to  $80 M_{\odot}$  lead to similar results for the two sets of yields

## Summary and Conclusions

[O/Mg], [Si/Mg] and [Ca/Mg] we find:

For rotating models:

- The ejected masses of all these element tend to increase because of the increase of the He core mass due to rotational mixing. This effect being different from star to star
- All these ratios are larger for lower mass models and lower for higher mass models . For [Fe/H]=0 negligible effect for the most massive stars
- No difference for the integrated [O/Mg] and [Si/Mg] at [Fe/H]=2, -1. Increase of 0.1-0.2 dex at [Fe/H]=0 compared to non rotating models
- Increase of integrated [Ca/Mg] by 0.2-0.3 dex compared to non rotating models at all metallicities